# **VOLATILIZATION OF ARSENIC AND ANTIMONY IN THE FIRE REFINING OF LEAD**

**By**

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**A thesis submitted to the Faculty and the Board of Trustees of the Colorado School of Mines in partial fulfillment of the requirements for the degree of Doctor of Science in Metallurgical Engineering.**

**Signed R. McClincy**

**Golden, Colorado**

Date:  $\frac{\gamma}{\mu\mu}$  22, 1968

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**Golden, Colorado Dates.** *U ( K y Z Z ,* **1968**

### ABSTRACT

The activity of  $\text{Sb}_{2}0_{3}$  in  $\text{Pb0-Sb}_{2}0_{3}$  slags containing less than 50 mole % Sb<sub>2</sub>0<sub>3</sub> was determined by the inert-gas satura**tion method at 700°C. In this composition range, the** activity of  $\text{Sb}_2\text{O}_3$  shows a strong negative deviation from ideality. The activity of Pb0 in Pb0-Sb<sub>2</sub>0<sub>3</sub> slags containing less than 50 mole  $\frac{1}{2}$  Sb<sub>2</sub>0<sub>3</sub> was calculated by application of the Gibbs-Dunem integration to the  $Sb_20_3$  activity data. **The activity of PbO in slags containing more than 63 mole % PbO is found to deviate in the positive direction from** ideality while for slags containing less than 63 mole % Pb0, **the activity of PbO deviates in the negative direction from ideality.**

The activity of  $\text{Sb}_{2}$ <sup>0</sup> in Pb0-Si0<sub>2</sub>-Sb<sub>2</sub><sup>0</sup> 3 ( $\frac{\text{Pb0}}{\text{S10}_{2}}$  = 2) slags containing less than 25 mole % Sb<sub>2</sub>0<sub>3</sub> was also determined by **the inert-gas saturation method at 700°C. In this composi**tion range, the activity of  $Sb_2^0$  shows a negative **deviation from ideality.**

**The vacuum removal of As and 5n as oxides from artificial lead-softening slags was shown not to be technically feasible at the concentrations and temperatures normally**

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**encountered in the conventional fire refining of lead. The** vacuum removal of Sb as  $Sb_20_3$  from artificial lead-softening slags was found to be a relatively fast, efficient method for the recovery of as much as  $80^{\circ}$  of the  $\mathrm{Sb}_2\mathrm{O}_3$  contained in **a 30 wt % Sb<sub>2</sub>0<sub>3</sub>-Si0<sub>2</sub>-Pb0 slag at 750°C. This removal was accomplished in 8 hr at 200y Hg pressure by adding 8-10** wt & Si0<sub>2</sub> to the slag. The condensate produced in this pro**cess contained 99 wt % Sb^Og.**

**The activity of As in Pb-As alloys containing less than 10 mole** *%* **As was determined by the inert-gas saturation method at 703°C. In this composition range, the activity of As exhibits near-ideal-solution behavior.**

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### **INTRODUCTION**

**The introduction to this investigation is presented in three parts: 1) the statement of the problem, outlining the subject of the investigation, 2) the organization of the problem, outlining the methods by which the problem was studied, and 3) the importance of the study, outlining the reasons for which the problem was studied.**

### **Statement of the Problem**

**This investigation makes a survey of the feasibility of** removing impurity oxides, Sb<sub>2</sub>0<sub>3</sub> in particular, from arti**ficial lead-softening slags under reduced pressure at elevated temperature. The impurity oxides are recovered as a pure, solid condensate. In order to describe more fully the results obtained, a thermodynamic activity study was** carried out on  $Sb_2^0$  dissolved in a slag of optimum compo**sition. Before any thermodynamic measurements could be made, however, it was necessary to design and construct a laboratory apparatus capable of determining vapor pressures** in the range of interest. The necessary equipment was con**structed and used to verify the available data in the**

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**literature for the vapor pressure of pure**  $\text{Sb}_{2}\text{O}_{3}$ **.** 

**Since arsenic is a common impurity in lead blast-furnace bullion and has an exceptionally high vapor pressure, a brief thermodynamic study was made on the Pb-As system at 700°C.**

### **Organization of the Problem**

**The problem was attacked experimentally by first making a survey of the relative rates of removal under reduced** pressure of  $As_{2}0_{3}$ ,  $Sb_{2}0_{3}$ , and  $Sn0_{2}$  from Pb0-based slags. **Artificial lead-softening slags containing the various impurity oxides singly or in combination were prepared and subjected to reduced pressure at various elevated tempera**tures. When it became apparent that  $only$   $Sb<sub>2</sub>0<sub>3</sub>$  showed an **appreciable rate of removal, fluxing agents, temperature, and pressure were varied in an effort to define a set of** optimum operating conditions for the removal of  $\text{Sb}_2^0$ <sub>3</sub>.

**The second portion of the investigation dealt with the measurement of certain thermodynamic properties of the slag systems. An apparatus was constructed to measure the vapor pressure of a volatile material over the range from 10~^ to " 3 10 atm. Vapor-pressure data for pure cadmium were obtained and compared with available data in the literature** to establish the reliability of the apparatus. A vaporpressure study on pure Sb<sub>2</sub>0<sub>3</sub> was then made to evaluate the

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**accuracy of the very limited data available in the literature for this compound. After the vapor pressure of pure SbgO^ was established, an activity study was conducted on** Sb<sub>2</sub>0<sub>3</sub> dissolved in an artificial lead-softening slag of the **optimum composition as defined by the vacuum-removal experiments.**

**The thermodynamic activity study on the Pb-As system was confined to dilute alloys of As dissolved in Pb for two reasons : 1) the vapor pressure of As^ above Pb-As alloys containing more than 3.5 wt % As exceeds the operating range of the experimental apparatus, and 2) the concentration of arsenic in normal lead blast-furnace bullion rarely exceeds 1 wt %.**

### **Importance of the Study**

**The commercial softening of lead blast-furnace bullion is accomplished either by selective oxidation of the impurities by using air and/or PbO as the oxidizing agent or by chemical means which produce a sodium antimonatc. In the former case, a high-antimony slag is produced which must be retreated in a reverberatory fuming operation or resmelted with carbon to produce an antimonial-lead product. The sodium antimonate produced in the latter case can be reduced to metal or converted into some other antimony com**pound, usually Sb<sub>203</sub>.

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**No work has yet been done to examine the feasibility of recovering antimony from lead-softening slags by the appli**cation of vacuum techniques. The experimental work involved **in this study provides a basis for the development of such a process. The vacuum removal of antimony from lead-softening slags could be desirable because both the time and temperature of slag treatment would be reduced, and the antimony would be recovered as a pure oxide without the necessity of extensive dust- and fume-recovery equipment.**

### **SURVEY OF THE LITERATURE**

**No studies are reported in the literature on the application of vacuum techniques to the treatment of leadsoftening slags. Other lead metallurgy processes involving the use of vacuum techniques such as the vacuum dezincing of lead bullion and Parkes1 crusts are well documented in the literature but do not bear directly on this study. Conventional lead softening and by-product recovery are represented in the published literature by a great many articles which are too numerous to mention individually.**

**A number of studies have been reported in the literature** that were concerned with the PbO-Sb<sub>2</sub>O<sub>3</sub> phase diagram. **Maier and Hincke (1932, p. 3-12) determined the melting**point diagram for the Pb0-Sb<sub>2</sub>0<sub>3</sub> system and identified the compound  $Pb0 \cdot Sb_2 0\frac{1}{3}$ . They found the phase diagram for this **system to be two simple eutectics located on either side of the single compound. They also determined a very limited** amount of vapor-pressure data for Sb<sub>2</sub>0<sub>3</sub> above Pb0-Sb<sub>2</sub>0<sub>3</sub> **melts at 69 7°C. A second phase-diagram investigation was done by Henning and Kohlmeyer (1957, p. 8-15) , who confirmed** the existence of the compound  $Pb0·Sb<sub>2</sub>0<sub>3</sub>$  as well as the form

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**of the diagram. A disagreement was noticed, however, in that their liquidas temperatures over nearly the entire diagram were higher than those reported by Maier and Hincke. Barthel (1957, p. 630) and Pelzel (1959, p. 558-561) redetermined the liquidas curve at the PbO-rich end of the** Pb0-Sb<sub>2</sub>0<sub>3</sub> system and agree very closely with the results of **Maier and Hincke. None of the investigators mentioned above** reported any mutual solid solubility in the PbO-Sb<sub>2</sub>0<sub>3</sub> **system. Zunkel and Larson (1967, p. 473-477) have determined** the phase diagram for the PbO-rich end of the PbO-Sb<sub>2</sub>O<sub>3</sub> system by slag-metal equilibria in the Pb-(PbO+Sb<sub>202</sub>) system and thermal analysis in the PbO-Sb<sub>2</sub>0<sub>3</sub> system. Their results **agree favorably with those of Maier and Hincke.**

**The vapor pressure of antimony trioxide in the temperature range from 470° to 800°C has been determined by Hincke (1930, p. 3869-3877). His results below the melting point are the only data reported in the published literature. Myzenkov and Klushin (1965, p. 1709-1718), using the boiling**point method, have determined the pressure of Sb<sub>4</sub>0<sub>6</sub> above liquid  $Sb_2^0$  in the temperature range from 715<sup>°</sup> to 1025<sup>°</sup>C. **The agreement between these two studies is not very close. A portion of the discrepancy lies in the fact that Hincke used silica crucibles which were attacked by the liquid SbgOg at high temperatures• This fact does not account, however, for the large difference at the melting point.**

**Maier (1934, p. 23) gives a brief summary of vapor-pressure** data for  $\text{Sb}_4^0$ <sup>6</sup> above pure liquid  $\text{Sb}_2^0$ <sub>3</sub>, which agree quite **well with the data of Myzenkov and Klushin at temperatures near the melting point.**

**Although arsenic has a very high vapor pressure and vacuum distillation appears to be a likely method for its removal from lead, the literature offers virtually no infor mation concerning the vacuum removal of arsenic from lead. Caldwell, Spendlove, and St. Clair (1960, p. 1-12) mention arsenic in their investigation on the removal of volatile metals from lead by vacuum distillation. They do not, however, give any data for arsenic removal or refer to any actual experimental work involving arsenic dissolved in lead.**

### **EXPERIMENTAL APPARATUS AND PROCEDURE**

**The experimental techniques used in this study required apparatus and procedures**

- **1) to determine the loss in weight of a sample in contact with a dynamic gas phase saturated with the vapor of the sample under conditions of constant but different inert-gas flow rates at a controlled, elevated temperature,**
- **2) to run distillation experiments on binary and ternary oxide systems in an inert atmosphere and at reduced pressure at a controlled, elevated temperature^**
- **3) to equilibrate slag-metal systems in an inert atmosphere at atmospheric pressure at a controlled elevated temperature,**
- **4) to analyze chemically the various phases produced in each experiment, and**
- **5) to analyze by X-ray diffraction techniques the slag and condensate phases produced in each experiment.**

### **Apparatus**

**The apparatus used in this study consisted of the transportation system for the inert-gas saturation experiments,**

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**the vacuum distillation system, which was used at atmospheric pressure for the slag-metal equilibration experiments and the X-ray diffraction system.**

**The. Transportation System. The transportation system, shown schematically in Fig. 1 and pictorially in Fig. 2, allowed for the equilibration of a 1- to 5-gm sample of a metal or oxide phase with an inert carrier gas stream moving at a known, constant flowrate. Experiments were carried out at atmospheric pressure at a controlled, elevated temperature.**

**The apparatus consisted of two separate gas-purification trains and a reaction system. In order to avoid any possible segregation of the carrier gas and the sample vapor due to large differences in molecular weight, argon was selected for the carrier gas. One gas-purification train admitted the argon carrier gas to the reaction system containing the sample to be studied, A second gas train admitted argon at a high flow rate to flush the volatile species away from the reaction zone. Both gas trains were constructed entirely of Pyrex brand glass tubing.**

**The gas purification train used for the inert carrier gas contained a flow meter for the measurement of the gas flow rate. After passage through the flow meter, the gas was led first through silica gel and then through anhydrous magnesium perchlorate drying chambers to remove most of the**

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Schematic Diagram of Transportation System Figure 1.

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# Figure 2. Photograph of Transportation System.

**water vapor. A mercury pressure-relief bubbler was placed in the gas train immediately upstream from the drying chambers to protect the system from any blockage. It was found that this method of gas purification was sufficient for the experiments involving vapor-pressure determinations on oxide systems. For the experiments involving metal samples it was found that a slight amount of surface oxidation took place. In order to eliminate this oxidation, the argon was mixed with about 1% of hydrogen. This argon/ hydrogen gas mixture was metered and dried as before. The gas mixture was then passed over pure copper wool at a temperature of 500°C to convert the residual oxygen to water vapor. The remainder of the purification train consisted of three anhydrous magnesium perchlorate drying chambers arranged in series to remove the water vapor.**

**The second gas-purification train used for the argon flushing gas contained a flow meter and silica gel and anhydrous magnesium perchlorate drying chambers. Since this gas did not come into direct contact with the sample, a high degree of purity was not required.**

**The reaction system, shown schematically in Fig. 3, was connected to the purification system by means of a short length of vacuum tubing. This connection was originally made with Tygon brand plastic tubing, but it was observed that sufficient water vapor diffused through the**



Schematic Diagram of Transportation Reaction System:<br>A-Tube Furnace, B-Alumina Winding Tube, C-Vycor Tube,<br>D-Cooling Coils, E-Alumina Reaction Tube, F-Boron<br>Nitride Plug, G-Sample, H-Combustion Tube Breech<br>Connector, I-Gas Figure 3.

**walls of the tube to recontarainate the carrier gas.**

**The carrier gas was admitted to the reaction system through a modified brass breech connector closing one end of a 11/16-in.-0D, 7/16-in.-ID by 24-in.-long high-purity** alumina reaction tube. The sample was placed in a 4-mm**wide by 25-mm-long by 4-mm-deep high-purity alumina combustion boat which fitted tightly into a plug which closed the other end of the alumina reaction tube. The plug was machined so as to provide a very close fit with the inside of the alumina reaction tube, and small channels were engraved on its surface to guide the carrier gas to the chamber containing the sample. The plug was constructed from HBR-grade boron nitride manufactured by the Union Carbide Corporation. The selection of boron nitride for the plug was made because of its inert nature, ease of machining, high-temperature dimensional stability, and resistance to thermal shock. A stainless steel pushrod was admitted through a viton O-ring seal in the modified breech connector to allow for the unloading of the reaction tube without opening the reaction system.**

**The reaction tube was placed inside a 45-mm-OD, 40-mm-ID by 36-in.- long Vycor brand glass tube. Closure was made, on one end, by a brass combustion-tube breech connector from which the sight glass had been removed and a Viton O-ring seal installed in its place. The breech**

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**connector was sealed into the end of the Vycor tube with a heat-resistant epoxy resin. The O-ring seal provided for a sliding seal between the alumina reaction tube and the Vycor tube by means of which the sample could be easily positioned once it was inside the furnace. The argon flushing gas was also admitted to the reaction system through the breech connector.**

**Closure on the other end of the Vycor tube was achieved by means of a rubber stopper. A standardized chrome1 alumel measuring thermocouple in a Vycor brand glass sheath and a gas outlet tube were positioned within the reaction** tube through the rubber stopper. All furnace gases exited **the transportation system through a dibutylphthalate bubbler.**

**The furnace used in this study was constructed from a 16-in.-diameter by 22-in.-long light-gauge, mild steel shell filled with diatomaceous earth insulation. The heating element consisted of 15 ft of 20-gauge nichrome wire and was supported by a 2^-in.-0D, 2-1/8-in.-ID by 22-in.-long mullite tube. The furnace assembly was closed on both ends by 3/ 8-in.-thick transite end plates held by four stainless steel tie rods. The heating element was wound nonuniformly so as to yield a 4-in.-long constant-temperature zone in which the temperature gradient did not exceed 0.5°C per linear inch in the temperature range from 250° to 750°C.**

**The furnace power was supplied by a Type 116 Powerstat**

**operating on 110 VAC. The furnace temperature was controlled by a Barber-Coleman Model 293C Capacitrol and a** 20-ft chromel-alumel thermocouple. A variable resistance **shunt was installed around the Capacitrol and adjusted to bypass 9 5% of the minimum furnace power required to maintain a given furnace temperature. The combination of the Capacitrol and the power shunt allowed for a maximum temperature variance within the furnace of ±1.5°C.**

**The Vacuum Distillation System. The vacuum distillation system shown schematically in Fig. 4 and pictorially in Fig. 5 allowed for the distillation of volatile oxides** from 500 gm of Pb0-SiO<sub>2</sub>-oxide slag in an inert atmosphere **at reduced pressure at a controlled, elevated temperature•**

**The distillation experiments were carried out in a 3<4-in.-OD, 2-3/4-in.-ID by 4^~in. -deep Type 416 stainless steel crucible. It was found that only the 400 series stainless steels would withstand the highly corrosive action of the slags at sustained high temperatures. Type 4 46 stainless steel was later found to be particularly resistant due to its ferritic rather than martensitic structure at high temperatures. The crucible was placed on an insulating firebrick pedestal located in the bottom of a vertically mounted 4-in.-ID, 4%-in.-OD by 13-in.-long fusedsilica reaction tube which was closed on the bottom end.** A condenser section composed of a  $3\frac{1}{2}-in.$ ID,  $3-3/4-in.$ -OD **by 12-in.-long fused-silica tube, open on both ends,**







Figure 5. Photograph of Vacuum Distillation System

**rested on an annular flange around the top of the stainless steel crucible. The condenser served to collect the products of volatilization and prevented any of the slag splashed out of the crucible from coming into contact with the fused-silica reaction tube. The reaction tube was closed on the open end by a water-cooled brass cap sealed by an annular silicone rubber gasket and an adjustable collar clamp. Connected to the brass cap were a sampling port, a takeoff for the introduction of inert gas, a takeoff to the vacuum pump, and a port housing a Teflon vacuum feed-through gland. A Type 416 stainless steel, motordriven paddle stirrer was introduced into the reaction tube through the vacuum feed-through gland.**

**A Lindberg Model 56622 crucible furnace with a 5-in.-ID by 8- in.-deep heating chamber was used as the source of heat. The furnace was capable of attaining a maximum temperature of 1210°C and maintaining a constant temperature zone of** *4%* **in. in the temperature range from 500° to 800°C. The furnace power was supplied by a Type 2 36 Powers tat operating on 220 VAC. A Barber-Coleman Model 293C Capacitrol and a 20-ft chromel-alumel thermocouple provided furnace temperature control to within ±3°C. The slag-meIt temperature was calibrated with the temperature scale on the controller to avoid having the thermocouple protection tube remain in contact with the highly corrosive slag for sustained periods**

**of time. The slag-melt temperature was periodically checked with-a calibrated chromel-alumel thermocouple enclosed in a protective Vycor tube to insure that significant temperature variations did not go unnoticed.**

**For the experiments operated at reduced pressure, a Duo-Seal Model. 1402B mechanical pump capable of producing a vacuum of ly Hg was used to produce a vacuum in the reaction tube. The vacuum level was periodically monitored by means of a McLeod gauge. The vacuum was controlled at the desired level by the introduction of argon through a modified reverse-taper Teflon stopcock. This method provided a control of ±15y Hg on the vacuum level.**

**For the experiments operated at atmospheric pressure, argon at 1 psig was allowed to flood the reaction tube through a valve in the inert-gas introduction system. Any leaks in the reaction system could be detected by observing the flow meter in the inert-gas introduction system.**

**Periodic sampling of the slag and metal phases was accomplished by inserting 7-mm Vycor tubes into the melt. The slags were sampled by inserting a sealed Vycor tube into the melt and immediately raising it. Approximately 1 gm of slag solidified on the tube and was scraped off and retained for chemical analysis. Samples of the metal phase were collected with a similar Vycor tube which had a small hole 3/8 in. above the sealed end. The sample tube was**
**lowered into the metal phase, allowed to fill, and quickly raised. The metal was then poured into cold water and the sample dried and retained for chemical analysis.**

**The X-ray Diffraction System. The X-ray analysis of the slag and condensate phases was accomplished by means of standard diffractometer procedures at room temperature.** All diffraction patterns were made with Cu  $K_{\alpha}$  radiation at **45 kv and 35 ma with appropriate rate-meter settings.**

### **Procedure**

**Three basically different types of experiments were conducted in this investigation: 1) vapor-pressure determinations on pure metals, alloys, pure oxides, and oxide slags, 2) rate-of-distillation experiments in an inert atmosphere at reduced pressure, and 3) slag-metal equilibrations in an inert atmosphere at atmospheric pressure. The samples collected during the experiments were analyzed to determine the composition of the slag and condensate phases and the impurity content of the metal.**

**Vapor-Pressure Determinations. The sample whose vapor pressure was to be determined was placed in the alumina combustion boat so as to fill it as completely as possible. The combustion boat was then inserted into the boron nitride plug which, in turn, was inserted into the open end of the alumina reaction tube. All loading operations were performed**

**against a strong flow of argon to prevent air from entering the system. A bypass line was installed in the flushing gas train to permit the introduction of argon from either end of the Vycor tube. The end of the reaction tube was positioned in the cold end of the Vycor tube for five minutes while a current of argon flushed away any air that might be present in the combustion boat. The reaction tube was then slid into the furnace and the cap of the combustion tube breech connector securely fastened. As soon as closure was effected, the argon bypass line was removed from the system by a pair of 3-way stopcocks and the flushing gas allowed to resume its normal flow. The final positioning of the sample within the furnace was effected by sliding the reaction tube through the O-ring seal in the cap of the breech connector. After the sample was in position, the carrier gas was turned off until the sample attained the proper temperature. When the sample had reached thermal equilibrium with the furnace, the carrier gas was turned up to the desired flow rate. This time was recorded as time zero for the experiment.**

**The time required for the sample to reach thermal equilibrium with the furnace varied as the character of the sample changed from metal to oxide and as the temperature of the experiments was increased. The amount of time required for the sample to heat up was determined separately** **T 1171 23**

**for each sample material at each temperature by embedding a standardized chromel-alumel thermocouple inside of a dummy sample. For the alloys and slags studied, weight losses during heat-up times were always negligible with respect to the total weight loss occurring during the experiment.**

**When a sufficient time had elapsed, the stainless steel push rod was used to slide the plug device to the end of the Vycor tube where the sample was cooled as rapidly as possible by a strong blast of air on the outside of the tube. Lead alloys originally at 700°C were observed to solidify within 30 seconds after unloading. The end of the experiment was recorded as the moment the plug was pushed out of the reaction tube.**

**After cooling for 5 minutes, the plug was removed from the Vycor tube and placed on a brass cooling block inside a dessicator. When the sample had reached room temperature, the combustion boat was weighed on a Mettler semimicro balance to determine its loss in weight during the experiment. The Mettler balance was capable of measuring weight changes of 1 mg accurately to** *1***%.**

**Sampling of the alloys and slags studied in this investigation was unnecessary due to the large differences in vapor pressure for the various components of the samples. In all cases, the observed weight losses could be attributed to only one volatile species.**

**The Pb~As alloys were prepared by melting the required amounts of lead and arsenic together under carbon powder in a graphite crucible in an inert atmosphere. (Reagent analyses are given in Appendix I.) The resulting alloy was then quickly cast into rods in a graphite mold and the mold** quenched in cold water. The Pb0-SiO<sub>2</sub>-Sb<sub>2</sub>O<sub>3</sub> slags were pre**pared by melting together the required amounts of PbO,** SiO<sub>2</sub>, and Sb<sub>2</sub>O<sub>3</sub> in a Type 446 stainless steel crucible in **the vacuum distillation apparatus under an inert atmosphere at atmospheric pressure. When the slag had been thoroughly mixed, the reaction system was quickly opened and the slag cast into a cast-iron mold which was then quenched in cold water. The alumina combustion boats were brought to constant weight by heating for 12 hours in a strong current of argon at 750°C.**

Rate-of-Distillation Experiments. The rate-of-distil**lation experiments were performed primarily on 500-gm** samples of the PbO-Sb<sub>2</sub>O<sub>3</sub> and PbO-SiO<sub>2</sub>-Sb<sub>2</sub>O<sub>3</sub> slags in the **vacuum-distillation apparatus under an inert atmosphere at reduced pressure. Reagents were mixed in the desired amounts and placed in the stainless steel crucible; the crucible was placed inside the fused silica reaction tube ; and the condenser was placed on the crucible. The stirring assembly was adjusted to a raised position in the brass cap, the cap was placed over the end of the reaction tube**

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**and clamped securely. After the vacuum line and the inert gas introduction line was connected by means of ball-and**socket joints, the system was evacuated to 50µ Hg and flushed **with argon eight times. After the last evacuation, argon at 1 psig was allowed to flood the system. The furnace, which had to be set at the desired temperature, was then raised into position around the reaction tube by means of a counter-weight system.**

**When the slag had reached the desired temperature, the stirrer was lowered into the melt and switched on, and the argon flow was turned off. The vacuum pump was turned on and the vacuum level adjusted by means of the Teflon leak valve. This time was recorded at time zero for the experiment, A vacuum of 200y Hg could be attained in about 30 seconds, and a level of 25y Hg required about 2 minutes.**

**Sampling of the slag was carried out at appropriate time intervals. When the last sample had been taken, the stirrer was switched off and raised out of the melt. The slag was then allowed to furnace cool under an inert atmosphere at atmospheric pressure to allow crystallization of the slag. When the solidification process was complete, the furnace was lowered, and the reaction system was allowed to air-cool to room temperature. After the entire system had cooled to room temperature, the argon flow was stopped; the brass cap and stirring assembly were**

**disconnected and removed; and the condenser and crucible were removed from the reaction tube. The condensate was chipped out of the condenser, weighed, and sampled; and the slag was sampled for X-ray diffraction analysis. The remaining slag was melted out of the crucible and cast into cakes.**

**Slag-Metal Equilibrations. The same general procedure as was described in the preceding section was used for the slag-metal equilibrations, with the exception that the experiments were carried out at atmospheric pressure. Approximately 18 hr were required for the establishment of equilibrium, and therefore sampling was carried out at 2-hr intervals after 18 hr until the analyses of two consecutive samples of both the slag and metal phases showed no significant change.**

**Analysis of the Slag, Condensate, and Metal Phases. Analyses of the slag and metal phases were performed by ASTM standard wet methods. The following methods of chemical analysis were used and are described in Appendix II:**

- **1) Sb and As in oxide slags — ASTM Standard Analysis E46-56, Arsenic and Antimony by the Disti11ation-Dromate Method.**
- **2) Sb dissolved in Pb same as 1) .**
- **3) Sn in oxide slags ASTM Standard Analysis E 57-6 0, Tin by the lodimetric Titration Method.**

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All  $Sb_2^0$ <sub>3</sub> condensate analyses were furnished through **the courtesy of the St. Joseph Lead Co., Monaca, Pennsylvania. An outline of their atomic absorption pro cedure is included in Appendix II. As was previously mentioned in the discussion of apparatus, the slags and condensates were analyzed by standard X-ray diffraction** procedures using Cu K<sub>ov</sub> radiation at room temperature.

### **EXPERIMENTAL RESULTS**

**The experimental results of this investigation are classified in four separate categories according to the type of experiment involved: 1) vapor-pressure determina**tions for Cd,  $Sb_2O_3$ , PbO-Sb<sub>2</sub>O<sub>3</sub> and PbO-SiO<sub>2</sub>-Sb<sub>2</sub>O<sub>3</sub> slags, **and Pb-As alloys, 2) rate-of-volatile-oxide-distillation** experiments in the  $Pb0-Me^{\chi 0}_{\chi}$  and  $Pb0-Si0^{\chi}_{2}-Me^{\chi 0}_{\chi}$  systems at **750° and 850°C, 3) slag-metal equilibrations in the** Pb- $( \text{Pb0+Si0}_2 + \text{Sb0}_3 )$  system at 700<sup>°</sup> and 750<sup>°</sup>C, and 4) results **of X-ray diffraction analyses on slags and condensates produced in experiments 2) and 3) .**

# Results from Vapor-Pressure Determinations for Cd,  $Sb_20_3$ ,  $Pb0-Sb<sub>2</sub>0<sub>3</sub>$  and  $Pb0-Si0<sub>2</sub>-Sb<sub>2</sub>0<sub>3</sub>$  Slags, and Pb-As Alloys

**The experimental results obtained from this portion of the investigation were obtained by determining the weight loss of a sample when a measured volume of inert gas at constant flow rate was passed over the sample in a known time at a known temperature. Due to large differences in the vapor pressures of the various components of the sample, the observed losses in weight of the sample could be**

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attributed solely to As for the Pb-As alloys and to  $Sb_2O_3$ for the  $Pb0-Si0^2-Sb^20^3$  and  $Pb0-Sb^20^3$  slags. A sample calculation for  $p_{Cd}$  above pure Cd is given in Appendix III.

**The standard deviation, normalized against the mean, for each vapor-pressure measurement was calculated and found** to lie within the limits  $0.00374 < \sigma' < 0.0433$ .

**Cadmium. In order to provide a check on the accuracy and reliability of the transportation apparatus constructed for this investigation, a brief vapor-pressure study was first made on a well known system. The results from the vapor-pressure determination experiments for Cd are shown in tabular form in Table 1 and graphically in Fig. 6 . The experimental data for these experiments are presented in tabular form in Appendix IV.**

Temperature	
Temperature, <sup>o</sup> C	$P_{Cd}$ , mm Hg
254	0.00534
297	0.0364
346	0.223
393	1.014

**Table 1. Vapor Pressure of Cadmium as a Function of Temperature**



Figure 6. Variation of log P<sub>Cd</sub> above Pure Cd with **Reciprocal Temperature**

Sb<sub>2</sub>0<sub>3</sub>. The results for this portion of the investiga**tion are presented in tabular form in Table 2 and shown** graphically in Fig. 7. The predominant vapor species has been shown to be  $\text{Sb}_{\Delta}$ <sup>0</sup>  $\text{c}_{\Delta}$  by Norman and Staley (1964, p. 1503). The vapor pressure of  $\text{Sb}_4^0$ <sup>6</sup> above pure, solid, cubic  $\text{Sb}_2^0$ <sup>3</sup> **was determined in the temperature range from 422° to 599°C.**

**Table 2. Vapor Pressure of Sb^O^ as a Function of Temperature**

Temperature, <sup>O</sup> C	$P_{Sb_40_6}$ , mm Hg
422	0.00162
454	0.00772
485	0.0277
514	0.0934
547	0.330
568	0.689
599	1.752

Pb0-Sb<sub>2</sub>0<sub>3</sub> Slags. The results for this portion of the **investigation are presented in tabular form in Table 3 and** shown graphically in Fig. 8. The vapor pressure of  $Sb_4^0^6$ was determined above Pb0-Sb<sub>2</sub>0<sub>3</sub> slags in the range from  $^{X}Sb_{2}0_{3} = 0.0442$  to 0.495 at 700°C. X-ray diffraction **analysis of the condensates produced in these experiments did not reveal the presence of any chemical species other**



**Figure 7.** Variation of  $\log P_{Sb_{4}0_{6}}$  above Cubic  $Sb_{2}0_{3}$  with **Reciprocal Temperature**

than  $Sb_20_3$ .

**Table 3. Vapor Pressure of Sb^Oç above PbO-Sb^O^ Slags at 700°C**

$x_{Sb_20}$ in slag	$P_{Sb_40_6}$ , nm Hg
0.0442	0.0304
0.108	0.0293
0.137	0.0290
0.176	0.0380
0.212	0.0560
0.280	0.126
0.495	1.235

Pb0-SiO<sub>2</sub>-Sb<sub>2</sub>O<sub>3</sub> Slags. The experimental results for **this portion of the investigation are presented in tabular form in Table 4 and shown graphically in Fig. 9. The vapor** pressure of  $\text{Sb}_{4}^{0}$  above Pb0-Si0<sub>2</sub>-Sb<sub>2</sub>0<sub>3</sub> slags was determined for the composition range from  $^{X}Sb_{2}0_{3} = 0.0296$  to 0.246 at **700°C. In order to keep this portion of the investigation within reasonable limits, a molar ratio corresponding to**  $\frac{200}{300}$  = 2 was selected and held constant throughout the **SiOz experiments. X-ray diffraction analysis of the condensates produced in these experiments did not reveal the presence** of any chemical species other than  $\text{Sb}_2^0$ <sub>3</sub>.



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**Figure <sup>8</sup>**. **Variation of log q above PbO-Sb^O^ Slags 4 6 with Composition at 700°C**

-	
$x_{Sb}^{}_{4}$ 0 <sub>6</sub> in slag	$P_{Sb_40_6}$ , mm Hg
0.0296	0.000537
0.0634	0.00275
0.0945	0.00766
0.130.	0.0265
0.167	0.0804
0.206	0.204
0.246	0.441

**Table** 4. **Vapor Pressure of Sb.Of** ft o **above Pb0-Si02-Sb203 (Pb0/Si02 =** 2) **Slags at** 700°C

**Pb-As Alloys, The results from this portion of the investigation are presented in tabular form in Table 5 and shown graphically in Fig. 10. The composition range covered was 0.01 to 0.09 mole fraction As dissolved in Pb at 70 3°C. Due to very small losses in weight for the samples containing 0.01425 mole fraction As, the calculated vapor pressure of arsenic above an alloy of this composition is only an approximation.**



 $\frac{\text{Pb0}}{\text{Si0}_2}$  = 2 Slags with Composition at 700°C

$X_{\text{As}}$ in alloy	$P_{\text{As}_{\text{A}}}$ above alloy, mm Hg
0,01425	0.00781
0.02794	0.0147
0.03805	0.0351
0.05265	0.0821
0.06901	0.238
0.08575	0.563

**Table 5. Vapor Pressure of As^ above Dilute Pb-As Alloys at 70 3°C**



**The results from this portion of the investigation were obtained by chemical analysis of the slags and condensates** produced by treating PbO-Me<sub>x</sub>O<sub>y</sub> and PbO-SiO<sub>2</sub>-Me<sub>x</sub>O<sub>y</sub> slag**forming mixtures under various conditions of temperature and pressure. The slag-phase analyses can be considered to be accurate to ±0.02 wt %.**

**Pb0-Mex0y Systems. Artificial lead-softening slags** containing approximately 3 wt  $%$  As<sub>2</sub><sup>0</sup><sub>3</sub>-97 wt  $%$  Pb0, 3 wt  $%$ As<sub>2</sub>0<sub>3</sub> - 30 wt %  $\text{Sb}_{2}$ 0<sub>3</sub> - 67 wt % Pb0, 30 wt %  $\text{Sb}_{2}$ 0<sub>3</sub> - 70 wt **& PbO, and 3 wt & As<sub>2</sub>0<sub>3</sub> - 10 wt & Sn0<sub>2</sub> - 30 wt & Sb<sub>2</sub>0<sub>3</sub> -57 wt % PbO were prepared and treated under various conditions of temperature and pressure. All experiments were**



Figure 10. Variation of log P<sub>As<sub>4</sub> above Dilute As-Pb Alloys</sub> **with Composition at 703 C**

**carried out under an argon atmosphere. The results from these experiments are given in Table 6 .**

Pb0-SiO<sub>2</sub>-Me<sub>x</sub>O<sub>y</sub> Systems. Based on the results of vacuum distillation experiments on the above  $Pb0-Me_{x}0_{y}$  systems, a **decision was made to limit experimental investigation of** silica additions to the Pb0-Si0<sub>2</sub>-Sb<sub>2</sub>0<sub>3</sub> system. Artificial lead-softening slags containing approximately 30 wt % Sb<sub>2</sub>0<sub>3</sub> and varying amounts of Pb0 and Si0<sub>2</sub> were prepared and **treated under various conditions of temperature and pressure. All experiments were carried out under an argon atmosphere. The results of these experiments are given in Table 7.**

## **Results from Slag-Metal Equilibrations in the Pb-(PbO+SiO2+Sb203) System at 700° and 750°C**

Selected slag compositions in the Pb0-Si0<sub>2</sub>-Sb<sub>2</sub>0<sub>3</sub> system **were equilibrated with Pb-Sb alloys at 700° and 750°C. The results from this portion of the investigation were obtained from the chemical analysis of the equilibrium metal and slag phases produced in each experiment. The experimental results** are shown in Table 8. The metal-phase analyses can be considered to be accurate to wt  $%$  Sb =  $\pm$  0.002.

### **Results from X-ray Diffraction Analysis of the Slags and Condensates**

**The various slags and condensates produced in a portion of the experiments in this investigation were analyzed by**



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**standard x-ray diffraction techniques to determine the compounds present. The x-ray diffraction analysis data are presented in Table 9, together with the compounds responsible for the diffraction peaks. The x-ray diffraction data for the pure compounds was taken from the ASTM Powder Data Index and are presented in tabular form in Appendix V.**

**Table 9. X-ray Diffraction Analysis of Slags and Condensates** Using Cu  $K_{\alpha}$  Radiation at Room Temperature

Test	$2 \theta$ , $^{\circ}$	Relative Intensity	Source of Peak
Condensate typical	13.84	W	Sb203
of the type produced	27.88	VS	$Sb_20_3$
where $%$ Sb <sub>2</sub> 0 <sub>3</sub> >95 $%$	23, 30	$\mathbf{m}$	Sb203
	28.53	W	$Sb_20_3$
	32.19	m	$Sb_20_3$
	35.17	W	
			$Sb_20_3$
Condensate typical	13.84	W	$Sb_20_3$
of the type pro-	27.88	VS	Sb203
duced where	28.30	m	$Sb_20_3$
$90\%$ $8Sb_20_3$ <95%	28.53	W	Sb203
	$28.67$ vw		Pb <sub>0</sub>
	31.35	W	Pb
	32.19	$\mathbf{m}$	$Sb_20_3$
	35.17	W	$Sb_20_3$
Condensate Test DD	13.91		
	22.81	VS.	As <sub>2</sub> 0 <sub>3</sub>
		w	As <sub>203</sub>
	28.02	VS	As <sub>2</sub> 0 <sub>3</sub>
	28.75	m	Pb <sub>0</sub>
	31.35	VS.	P <sub>b</sub>
	32.40	$\mathbf{m}$	As <sub>2</sub> 0 <sub>3</sub>
	35.41	S	As <sub>2</sub> 0 <sub>3</sub>
	36.35	$\mathbf{m}$	Pb

**Test 2 Q,° Relative Source of Peak Intensity Slag - Test F Slag - Test G Slag - Test E**  $27.52 \t m$  **(Pb0**  $5b_203$ ) \* 28.30 **vs**  $Pb0, Sb203$ <br>29.38 **w**  $(Pb0 \cdot Sb203)$ **29.38 w (Pb0«Sb203) , PbO 31.30 w Pb 0, Pb 32.58 s PbO**  $33.29$  **w**  $(Pb0 \cdot Sb_2 03)$  $34.10$  vw (Pb0 $\cdot$ Sb<sub>2</sub>0<sub>3</sub>) **35. 40 vw PbO 36.21 vw PbO** 27.74 m (Pb0\*Sb<sub>2</sub>0<sub>3</sub>) **28.20** vs Pbo,  $\frac{5}{2}0\frac{3}{3}$ 29.48 w  $(Pb0 \cdot Sb203)$ , Pb0 **29.83 vw - - - 31.37 vw P b O , Pb 32.53 s PbO 33.48** w  $(Pb0 \cdot Sb_2 0_3)$ **36.14 vw PbO 27.65 m** (Pb0\*Sb<sub>2</sub>03), As<sub>2</sub>03 m 28.35 **vs** Pb0,  $\frac{35}{29.31}$  **vs** Pb0,  $\frac{35}{203}$ **29.31 29.31 29.31 20.31 20.32 20.32 20.32 20.32 20.32 20.32 29.72 v**w **(Pb0**•Sb<sub>2</sub>0<sub>3</sub>) **30.02 vw — 31.28 w Pb0, Pb**<br>**32.67 s Pb0, As 32.67** s Pb0,  $\text{As}_2\text{O}_3$ <br>**33.38** w (Pb0.Sb<sub>2</sub>0<sub>3</sub>) **33.38 w (Pb0.Sb<sub>2</sub>03)<br><b>34.00 <b>w (Pb0.Sb**<sub>2</sub>03) **34.00 vv** (Pb0 · Sb<sub>2</sub>0 3) **35.43 w PbO**,  $\text{As}_2^0\text{O}_3^3$ **27.78 s** (Pb0•Sb<sub>2</sub>0<sub>3</sub>)<br>28.32 **vs** Pb0, Sb<sub>2</sub>0<sub>3</sub> 23.32 **vs** Pb0, Sb<sub>2</sub>0<sub>3</sub><br>29.59 **m** (Pb0·Sb<sub>2</sub>0<sub>3</sub>)  $\text{Im} \quad \text{(Pb0-Sb)}\left(\frac{1}{2}\right)$ **30.50 w PbO 31. 59 m PbO, Pb 32. 80 El PbO**  $34.29$  **m** (Pb0\*Sb<sub>2</sub>0<sub>3</sub>) **36.32 w PbO**

**Table 9« Cont'd**

**\*No standard pattern available in ASTM Powder Data Index, see Appendix VI.**

Table 9. Cont'd

1001070 ovno u Test	$2 \theta$ , $^{\circ}$	Relative Intensity	Source of Peak
$Slag - Test U$	26,60 28.27 29.38 31.38 32.88 34.02 36.32	VV. $S_{-}$ VW m m m W.	Sn02 Pb0, Sb203 $(Pb0 \cdot Sb_2 0_3)$ , Pb0 Pb0, Po Pb0 $(Pb0 \cdot Sb_20_3)$ Pb0
$Slag - Test AA$	27.45 27.97 29,67 31.42 33.67 34.40 36.69	VV I $\mathbf{s}$ VS W. m m VV.	$(Pb0 \cdot Sb_20_3)$ $(Pb0'Sb203)$ , Pb0 Pb0, Pb $(\text{Pb0} \cdot \text{Sb}_2 0_3)$ (Pb0 $\cdot$ Sb <sub>2</sub> 03) Pb0
$Slag - Test BB$	27.62 28.31 29.58 30.30 31.40 32.10 32.87 33.30 34.29 35.58 36.40	$S_{-}$ S m W. W VW m W W V W	$(Pb0 \cdot Sb_20_3)$ Pb0, $Sb_2^0c_3$ $(Pb0 \cdot Sb_2^003)$ , Pb0 Pb0 Pb0, Pb $Sb_20_3$ , (Pb0. $Sb_20_3$ ) $\overline{0}$ d $(Pb0 \cdot Sb_20_3)$ $(Pb0 \cdot Sb_20_3)$ P <sub>b</sub> 0 Pb <sub>0</sub>
$Slag - Test CC$	28.22 28.62 29.73 30.38 31.50 33.17 34.50 35.75	<b>VM</b> <b>VS</b> W VW VW ${\bf m}$ W V	Pb0, $Sb_203$ Pb0, $Sb_20_3$ $(Pb0 \cdot Sb_2 0_3)$ Pb <sub>0</sub> Pb0, Pb $\mathrm{Sb}_20_3$ , $(\mathrm{Pb0 \cdot Sb}_20_3)$ $(Pb0.5b_20_3)$ P <sub>D</sub> <sub>0</sub>
$Slag - Test DD$	28.12 28.88 29.27 30.28 31.17 31.40 32.00 33.45 35.70	s S W m m W W m	Pb0 Pb0 Pb0 Pb Pb0 Pb0

**Table 9« Cont'd**

Test	$2 \theta$ , $^{\circ}$	Relative Intensity	Source of Peak
Slag - Test GG	26.80 27.60 28.33 29.38 30.10 31.30 32.87 33.20 34.10 35.50 36.28	VW. $\mathbf{s}$ VS. W VVI. W m W. VV VVI VV.	$(Pb0 \cdot Sb_20_3)$ $(Pb0 \cdot Sb_20_3)$ Pb0, $Sb_20_3$ $(Pb0 \cdot Sb_2^00_3)$ Pb0 Pb Pb0 $(Pb0 \cdot Sb_20_3)$ $(Pb0 \cdot Sb_2^00_3)$ Pb <sub>0</sub> $(Pb0 \cdot Sb_20_3)$
Slag typical of Tests HII, II, JJ, $LL$ , $MM$ , and $NN$	27.77 28.30 31.40 32.80 33.30 35.60 36.38	m VS variable m W VVI VW	$(Pb0 \cdot Sb_20_3)$ $Pb0, Sb_20_3$ P <sub>b</sub> Pb <sub>0</sub> $(Pb0 \cdot Sb_20_3)$ Pb0 $(Pb0 \cdot Sb_20_3)$
$Slag - TestS RR$ and SS	28.08 28.58 29.60 30.00 30.81 31.50 32.54 33.18 33.50 36.50	s VS W W W m W m W. VV <sub></sub>	$Sb_20_3$ $\gamma$ -4Pb0.Si02 $\gamma$ -4Pb0 · Si0 $\overline{2}$ $\gamma - 4Pb0 \cdot Si0_2$ $\gamma - 4Pb0 \cdot Si07$ $\gamma$ -4Pb0 $\cdot$ Si0 $\overline{2}$ Sb203 $\gamma - 4Pb0 \cdot Si02$ $\gamma - 4Pb0 \cdot Si0_2$ Pb <sub>0</sub>
Slag - Tests VV and WW	21.67 23.12 25.72 28,50 29.72 30.44 31.60 31.80 32.58 33.05 33.72 34.40	w W W VS m m m m $\mathfrak{m}$ $\mathfrak m$ m m	2 Pb $0.5i02$ 2 Pb0 $\cdot$ Si0 $\overline{2}$ 2 Pb0 $\cdot$ Si0 $\frac{1}{2}$ $\gamma - 4Pb0 \cdot Si\bar{0}$ 2, $\mathrm{Sb}_20_3$ , $2\bar{P}b0.5i0_2$ $\gamma$ -4Pb0.Si0 <sub>2</sub> , 2Pb0.Si0 <sub>2</sub> $\gamma$ -4Pb0 $\cdot$ Si0 $\frac{1}{2}$ , $2Pb0 \cdot Si0_2$ $\gamma$ -4Pb0.Si0 $\overline{2}$ $2Pb0 \cdot Si02$ $\gamma$ -4Pb0.Si02, Sb203 $\gamma - 4Pb0 \cdot Si02$ , $Sb203$ $\gamma$ -4Pb0·Si0 <sub>2</sub> , Sb <sub>2</sub> 0 <sub>3</sub> $2Pb0 \cdot Si0_2$

Table 9. Cont'd

Table 9. Cont'd Test	$2 \theta$ , $^{\circ}$	Relative Intensity	Source of Peak	
$flag - Tests PP,$ $QQ$ , $AB$ , and AC	21.43 22.95 25.60 28.20 29.63 30.18 31.58 32.60	W W W VS W m m variable	$2Pb0 \cdot Si02$ $2Pb0 \cdot Si0_2^-$ $2Pb0 \cdot Si02$ $2Pb0.5i02$ , $Sb203$ 2Pb0.5i0 <sub>2</sub> $2Pb0 \cdot Si0_2$ $2Pb0 \cdot Si02$ $Sb_20_3$	
$flag - Test XX$ and YY	20.83 23.92 25.19 27.27 27.61 28.30 29.25 30.10 31.10 31.40 31.85	w W W m $\mathbf{s}$ m m m $S_{-}$ VS. s	$Pb0 \cdot Si02$ $Pb0 \cdot Si02$ $Pb0 \cdot Si0_2$ Pb0.5i07 $2Pb0 \cdot Si\overline{0}_2$ , $Sb_20_3$ $2Pb0 \cdot Si0_2$ , $Pb\overline{0} \cdot \overline{S}i0_2$ $2Pb0 \cdot Si0_2$ , $Pb0 \cdot Si0_2$ $Pb0 \cdot Si02$ $Pb0 \cdot Si02$ Pb0.5i0 <sub>2</sub>	
Slag - Tests TT and UU	$34^\circ$ 20.		These slags produced diffraction patterns typical of vitreous materials. They consisted of one broad, low peak extending approximately from 24 <sup>0</sup> to	
$Slag - Tests BA$ and BB	27.83 28.71 29.91 31.33 32.17 $Pb0 \cdot Si0_2$	m W W W W	$2Pb0-Si02$ $2Pb0 \cdot Si0_2$ $2Pb0 \cdot Si02$ $2Pb0 \cdot Si02$ $2Pb0 \cdot Si02$ The diffraction peaks were nearly masked by a broad, low peak extend- ing approximately from 24 <sup>0</sup> to 34 <sup>0</sup> 20 indicating non-crystallization of	

$\cdots$ Test	$2 \theta$ , $^{\circ}$	Relative Intensity	Source of Peak
$Slag - TestB BC$	21.32	W	$2Pb0 \cdot Si02$
and BD	22.87	W	
	24.00	W	$2Pb0 \cdot Si02$
	25.50	W	$2Pb0 \cdot Si02$
	27.82	VS	$2Pb0 \cdot Si02$ , $Sb203$
	28.22	VS	$\gamma - 4Pb0 \cdot 5i0$
	29.50	S	$\gamma$ -4Pb0.Si0 <sub>2</sub> , 2Pb0.Si0 <sub>2</sub>
	30.02	m	$\gamma$ -4Pb0.Si02, 2Pb0.Si02
	31.50	W	$2Pb0 \cdot Si02$
	32.27	W	
	32.75	W	$\gamma$ -4Pb0. Si0 <sub>2</sub>
	33.40	W	
	33.80	W	$\gamma - 4Pb0 \cdot Si02$
	34.77	W	$2Pb0 \cdot Si0_2$
$Slag - Tests BE$	21.12	W	$2Pb0 \cdot Si02$
and BF	22,80	w	
	24.03	W	$2Pb0 \cdot Si02$
	25.48	W	$2Pb0 \cdot Si02$
	27.75	W	$2Pb0 \cdot Si02$ , $Sb203$
	28.00	m	
	28.74	VS	$2Pb0 \cdot Si02$
	29.70	W	$2Pb0 \cdot Si02$
	31.28	W	$2Pb0 \cdot Si02$
	31.80	W	$2Pb0 \cdot Si02$
	32.40	W	
	33.27	W	
	34.75	W	$2Pb0 \cdot Si02$

**Table 9» Cont'd**

#### CALCULATIONS AND INTERPRETATION OF RESULTS

**The discussion of the experimental results obtained in this investigation is presented in six sections : 1) the use of the transportation technique for the measurement of vapor pressures, 2) the vapor pressure of**  $Sb_20_3$  **in the range from 422° to 599°C, 3) the evaluation of vapor-pressure data for the determination of thermodynamic data for** Pb0-Sb<sub>2</sub><sup>0</sup><sub>3</sub> and Pb0-Si0<sub>2</sub>-Sb<sub>2</sub><sup>0</sup><sub>3</sub> slags at 700<sup>o</sup>C, 4) the application of vacuum techniques to the removal of  $As_2O_3$ ,  $Sb_2O_3$ , **and Sn02 from lead-softening slags, 5) selected slag-metal** equilibria in the Pb0-SiO<sub>2</sub>-Sb<sub>2</sub>O<sub>3</sub> system, and 6) the vapor **pressure of As4 above dilute Pb-As alloys at 70 3°C.**

## Use of the Transportation Technique for the Measurement **of Vapor Pressures**

**The transportation technique, or inert-gas saturation method, for the measurement of vapor pressures has been in general use for many years. The published literature contains accounts of a great many experimental investigations using this technique, investigations which are far too numerous to list here. In the past, the design of the**

**apparatus and the size of the sample to be studied have been largely the choice of the individual worker. Not** until the work of Alcock and Hooper (1959, p. 325-340) has **there been any attempt to establish criteria by which the accuracy and. reliability of the method could be estimated.**

**The design of the experimental apparatus used in this investigation is based largely on the apparatus used by Alcock and Hooper, Certain modifications were made in the basic design to provide more thorough carrier-gas purification and to provide greater ease in sample handling. The sample geometry is essentially the same as that used by Alcock and Hooper. Figure 3, p. 13, illustrates the con**ditions under which the experiments were made. A sample, **weighing between 1 and 5 gm, is held in a small combustion boat which rests in a recess in a plug device. The recess in the plug was machined to conform to the outside contours of the combustion boat in order to reduce the dead volume between the boat and the plug to a minimum. For reasons to be explained later, the sample must be made to fill the space between the boat and the reaction tube as completely as possible. The plug containing the sample is then placed in the open end of the reaction tube. It is necessary to provide as tight a seal as possible between the plug and the reaction tube. Careful lapping of the inside surface of the reaction tube can result in a nearly air-tight seal**

**at room temperature. Small channels were engraved on the top surface of the up-stream end of the plug to provide an entrance to the sample chamber for the carrier gas. A single channel provided the necessary exit at the other end of the plug.**

**When the above precautions are taken, it can be reasonably assumed that the carrier gas passes over the sample to be studied and not around the sides and/or bottom of the plug. In passing over the sample, the carrier gas accumulates the vapor of the sample and carries it out of the reaction system. The amount of volatile matter removed from the sample is determined as the loss in weight of the sample and is normalized against a unit volume of carrier gas. By plotting the normalized weight-losses measured at different flow rates against flow rate, a curve similar to that shown in Figure 11 is obtained.**

**The curve shown in Figure 11 represents a somewhat idealized case. It can be readily divided into three separate sections whose slope is controlled by three different phenomena. Section I shows a smooth decrease in the normalized weight loss from very small carrier-gas flow** rates up to some given value, say f<sub>1</sub>. Section II shows **that the normalized weight-loss remains constant at all values of carrier-gas flow rate between the limits f^ and** f<sub>2</sub>. This portion of the curve corresponds to the true




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**vapor pressure of the sample. Section III shows an increasingly rapid decrease in the normalized weight-loss as the carrier-gas flow rate is increased above the value repre**sented by the point f<sub>2</sub> in Figure 11.

**The cause of the abnormally high weight losses at low flow rates can be thought of as being three-fold: 1) a large difference in molecular weight between the volatile species and the inert carrier gas provides for a tendency for the various molecular species to segregate from one another, 2) the existing thermal gradients on either side of the sample will result in a mass flux of one of the vapor species relative to the other as a result of thermal diffusion, and 3) the concentration gradients set up on either side of the sample will give rise to a diffusive mass flux of one of the vapor species relative to the other.**

**In the first case, actual physical segregation of the vapor species due to differences in molecular weight can be neglected for two reasons : 1) the carrier gas is moving over the sample with a relatively high velocity so that the retention time above the sample is small and 2) obstacles such as the uneven surface of solid samples, or artificial baffles in the case of liquid samples, serve to provide a maximum amount of turbulence in the gas phase.**

**Thermal diffusion, as a rule, provides for only a minimal degree of vapor segregation unless the thermal**

**gradient is quite large. Such large differences in temperature in the vicinity of the sample are not to be expected under normal conditions. In order to illustrate the magnitude of this contribution, a calculation will be made** for the binary vapor system  $argon-Sb_40_6$ .

**A temperature gradient in the system will give rise to a** mass flux of  $Sb_4^0$ <sup>6</sup> given by:

$$
j_{\text{Sb}_40_6} z = -\frac{c^2}{\rho} M_{\text{Sb}_40_6} M_{\text{A}} D_{\text{Sb}_40_{6-\bar{\text{A}}}} \frac{k_{\text{T}}}{\text{T}} \frac{d\text{T}}{dz}
$$
 (1)  
where:  $j_{\text{Sb}_40_6} z$  = mass flux of  $\text{Sb}_40_6$ ,  $\text{gn/sec-cm}^2$   
 $c = \text{total molar concentration, mols/cm}^3$   
 $M_i$  = molecular weight of species i, gm/mol  
 $D_{\text{Sb}_40_6} A$  = binary diffusivity for system  
 $S_{\text{b}_40_6 - \text{A}_6} \text{ cm}^2/\text{sec}$   
 $k_{\text{T}}$  = thermal diffusion ratio  
 $\text{T} = \text{temperature, } {}^{\text{O}}\text{x}$   
 $\rho = \text{fluid density, gm/cm}^3$   
 $d\text{T}/dz$  = temperature gradient,  ${}^{\text{O}}\text{K}/\text{cm}$ 

**This mass flux will set up a concentration gradient which will result in an opposing mass flux:**

$$
\mathbf{J}_{\mathrm{Sb}_4 0_6}^{(x)} \mathbf{z} = \frac{c^2}{\rho} \, \mathbf{M}_{\mathrm{Sb}_4 0_6} \, \mathbf{M}_{\mathrm{A}} \, \mathbf{D}_{\mathrm{Sb}_4 0_6} - \mathbf{A} \, \frac{\mathbf{dx}_{\mathrm{Sb}_4 0_6}}{\mathbf{dz}} \tag{2}
$$

In this case  $\frac{dx}{dx}$  <sup>dx</sup>  $\frac{dy}{dx}$  <sup>0</sup> 3/dz refers to the concentration grad**ient expressed in mois/cm. When steady-state conditions have been attained, the two opposing mass fluxes will**

**nullify one another**

$$
0 = j_{Sb_40_6}^{(t)}, z + j_{Sb_40_6}^{(x)} z = \frac{c^2}{\rho} M_{Sb_40_6} M_A D_{Sb_40_6} - A
$$

$$
\left[ \frac{dx_{Sb_40_6}}{dz} + \frac{k_{T}}{T} \frac{dT}{dz} \right]
$$
(3)

**from which,**

$$
dx_{\rm Sb}^{\dagger}{}_{4}^{\dagger}{}_{6}^{\dagger} = -\frac{k_{\rm T}}{\rm T} d\rm T
$$
 (4)

From Equation (4) it is seen that, when  $k_T$  is positive, Sb<sub>4</sub>0<sub>6</sub> will move towards increasingly lower temperatures; and when  $k_T$  is negative,  $Sb_40_6$  will move towards increas**ingly higher temperatures. In order to integrate Equation (4) it will be assumed that k™ is constant with composition** if the mass flux is small. Also, since  $k_{\phi}$  varies in a **complex manner with temperature, it will be assumed to be independent of temperature for small temperature gradients.** By use of these assumptions, then, Equation (4) can be **integrated as follows ;**

$$
\int_{X_{\text{Sb}_40_6}^1}^{X_{\text{Sb}_40_6}^1} \, \mathrm{d}x_{\text{Sb}_40_6} = -k_{\text{T}} \int_{\text{T}_1}^{\text{T}_2} \, \frac{\mathrm{d}r}{\mathrm{T}} \tag{5}
$$

**from which,**

$$
X''_{Sb_40_6} - X'_{Sb_40_6} = k_{T} ln \frac{T_2}{T_1}
$$
 (6)

**Before Equation (6) can be solved, it is necessary to evalu** ate the thermal diffusion ratio, k<sub>p</sub>. Gillespie (1939, p. **530-5) has derived an expression for in terms of the** square roots of the molecular weights,  $m_i$ , and the mole fractions,  $X_i$ , of the species in a binary system with the **result that:**

$$
k_{\text{T}} = \frac{\frac{1}{2} \left( \frac{M_{\text{A}}}{M_{\text{S}} b_{4} 0_{6}} - 1 \right) X_{\text{A}}}{1 + \frac{M_{\text{A}}}{M_{\text{S}} b_{4} 0_{6}} \cdot \frac{X_{\text{A}}}{X_{\text{B}} b_{4} 0_{6}}}
$$
(7)

For purposes of calculation, the mole fraction of  $\text{Sb}_4\text{0}_6$  is responds to a partial pressure of  $Sb_40_6$  of 1 mm Hg. Sub**stitution of this data together with the appropriate molecu-**Since k<sub>n</sub> is negative, it is readily seen from Equation (6) that  $Sb^0$ <sub>6</sub> will tend to diffuse to a region of higher **temperature under the influence of a temperature gradient. Thermal diffusion, then, cannot be responsible for the abnormally high weight losses observed at low flow rates.** The negative value of  $k_{\text{th}}$  would tend to cause abnormally low **weight losses rather than higher.**  $\alpha$  chosen as  $X_{\text{Sh},40}$  =  $1.6$  x  $10^{-3}$ , and the total pressure of the  $\texttt{system}$  is taken to be 1 atm. This value for  $\text{X}_{\text{Sh}_A 0_A}$  corlar weights into Equation (7) yields  $k_T = -2.8 \times 10^{-3}$ .

**The significance of this back diffusion, however, is** of little importance. At a mean temperature of 700<sup>o</sup>C, a

**temperature gradient of 2° to 3°C from the sample to the mouth of the reaction tube would result in a concentration**  $difference, X''$ Sb<sub>4</sub>0<sub>6</sub> -  $X'$ Sb<sub>4</sub>0<sub>6</sub>, of only 8.4 x 10<sup>-6</sup> mole fraction, which is less than  $0.1\%$  of  $X_{\text{Sb}_406}$ <sup>\*</sup>

**The third possible explanation for the abnormally high weight losses observed at low flow rates involves the concentration gradients established in the vicinity of the sample. If the gas phase is assumed to be stationary, it can be reasoned that very steep concentration gradients exist between the space immediately above the sample and the gas film surrounding the plug at the beginning of the experiment. Before this mass flux is calculated by means of Equation (2), it is necessary to estimate the binary**  $\texttt{diffusivity, } \texttt{D}_{\text{Sb}_4^00}$  , for the system  $\texttt{Sb}_4^0\texttt{6}$ -argon

**Several methods are available for estimating binary diffusivities. The most accurate method is based on the Chapman-Enskog kinetic theory. The resulting equation can be represented as follows : -3**  $(8)$  $\mu_{\text{Sb}_40}$ <sup>2</sup>A = 1.858 x 10

**where: p = pressure of the system, atm o collision diameter, A**  $\Omega_{D}$ , Sb  $_{4}$ <sup>0</sup>  $_{6-A}$ = dimensionless function of the temperature and **of the intermolecular potential field for one molecule of each species**

**4 6-A**

The collision diameter,  ${}^{\sigma} \text{Sb}_{4} {}^{0}{}_{6-\text{A}}$ , must be approximated by **the sum of the molecular radii. Norman and Staley (196 4, p. 1503-4)** have shown that  $Sb_40_6$  is composed of tetrahedrally**located Sb atoms, with each oxygen atom associated with an o edge of the tetrahedron. The Sb-Sb distance is 3.61 A and will be used as the approximate molecular diameter. The atomic diameter of argon, as calculated from the Van der o Waal's equation, is 2.9 4 A. By the assumption that the molecules behave as elastic, hard spheres, ^U,Sb^0^"^ can be set equal to unity.**

**Substitution of the appropriate values into Equation** (8) using  $p = 1$  atm and  $T = 973^{\circ}K$  yields: **o**  $D_{\mathrm{Sh}}$  n = 0.861 cm<sup>2</sup>/sec

Therefore, using the above values for  $X_{Sb_40_6}$ ,  $M_{Sb_40_6}$ ,  $M_A$ , **and q Equation (2) becomes,**  $4^{\circ}$ 6-A

$$
j_{\rm Sb_{4}0_{6,Z}}^{(x)} = -6.18 \times 10^{-3} \frac{d x_{\rm Sb_{4}0_{6}}}{dz}
$$
 (9)

Integrating Equation (9) over the limits  $X^{\mathbf{w}}$ Sb<sub>A</sub>O<sub>6</sub> = 0 to  $X'_{Sb}^{0}$  = 2 x 10<sup>-3</sup> and z" = 0.25 cm to Z' = 0.0 cm yields **4.9 4 x 10"5 gm/sec-cm3 initially. This mass flux will of course decrease with time towards some steady-state value. If the total cross-sectional area between the plug and the reaction tube is taken to be 0.2**  $cm<sup>2</sup>$ **, the mass flux due to diffusion can be shown to be as much as 20% of the weight**

**losses observed in experiments made with a carrier-gas** flow rate of 100  $\text{cm}^3/\text{min}$  where  $p_{\text{Sb}_40}^{\text{}}$  = 1 mm Hg. At the **point represented by flow rate f^, in Figure 11, the carrier gas is flowing over the sample at the minimum rate capable of sweeping away all of the diffusional mass** flux of  $Sb_40_6$  produced by the zero-time concentration **gradient. By use of the above calculated flux, this minimum flow rate is calculated to be 50 cm^/min. The actual flow rate at which the normalized weight-loss versus flowrate curve becomes horizontal for £5^ q approximately 4 6 equal to 1 mm Hg is slightly above this value for the experiments performed in this investigation.**

**Considering the assumptions and approximations made in** calculating the diffusional mass flux of  $\text{Sb}_4\text{O}_6$ , it would **appear that this flux is of the correct order of magnitude to cause the abnormally high normalized weight losses observed at low carrier gas flow rate.**

**Referring again to Figure 11, it is seen that Section II of the curve has zero slope. This condition is explained** by the fact that at all flow rates between  $f_1$  and  $f_2$  the **carrier gas is able to become saturated with the volatile species from the sample. The diffusional mass flux of the volatile species is not sufficiently rapid to affect the removal of these species from the reaction zone by the rapidly moving carrier-gas stream.**

**Section III of the curve in Figure 11 is due to the carrier gas moving at too rapid a rate over the sample to allow for complete saturation. As the carrier gas flow** rate increases from f<sub>2</sub>, the degree of undersaturation **increases and the normalized weight-loss of the sample falls to lower values.**

**As mentioned earlier, the curve shown in Figure 11 represents a somewhat idealized case. In order to obtain a curve of the required form, i.e. a curve showing the normalized sample weight-loss to be independent of carriergas flow rate over a range of flow rates, it is necessary to reduce the dead volume above the sample to a minimum. When this condition is not met, the horizontal segment of the normalized weight-loss versus flow-rate curve will either assume a finite slope or disappear altogether. Figure 12 illustrates this phenomenon for 2 series of** experiments made on pure  $\text{Sb}_2^0$ <sub>3</sub>at 514°C. In one case, the **sample extended above the top of the combustion boat to insure a small dead volume in the reaction system and a curve of the desired form was obtained.**

**For the experimental results represented by the second curve, the sample extended to slightly above the center of the combustion boat, resulting in a relatively large dead volume above the sample. It can readily be seen that the curve shows a smoothly decreasing normalized weight-loss**



**with Increasing carrier-gas flow rate over the entire range of flow rates studied. The true vapor pressure of the sample cannot even be estimated from these data.**

**In order to provide a check on the accuracy and reliability of the transportation apparatus constructed for this investigation, a brief vapor-pressure study was first made on a well known system. Cadmium was chosen for the reference study for three primary reasons : 1) the literature contains a large number of vapor-pressure studies on Cd which are in good agreement with one another; 2) Cd possesses a vapor pressure in the range expected in the** other studies reported in this investigation  $(10^{-3} - 10^{-6})$ **atm); and, 3) Cd is readily available in very pure form.**

**A total of four vapor-pressure measurements were made on Cd in this investigation; two for the vapor pressure above solid Cd, and two for the vapor pressure above liquid Cd. The results of these measurements are shown graphically in Figures 13 and 14. Two factors concerning the shape of these curves are readily apparent. Firstly, the length of the horizontal portion of the curves decreases with an increase in the absolute magnitude of the vapor pressure. This is to be expected since saturation of the gas phase at high flow rates becomes more difficult as the total mass of volatile species increases. The second observation to be made is that the horizontal portion of the curves shifts to**



**Figure 13. Weight of Cd Lost per Liter of Carrier Gas as a Function of Flow Rate at 254° and 29 7°C**

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**Figure 14. Weight of Cd lost per Liter of Carrier Gas as a Function of Flow Rate at 346° and 393°C**

**lower flow rates as the magnitude of the vapor pressure increases. This type of behavior is explained by the fact that the effects of mass diffusion are more easily overcome at higher mass densities of the volatile species «**

**The vapor pressures of Cd at various selected temperatures, as calculated from the data of Figures 13 and 14, are presented in Figure 15 together with a portion of the literature data for the vapor pressure of Cd. All available data have not been included in Figure 15 for the purpose of clarity. The agreement for the vapor pressure of Cd at temperatures above the melting point of Cd with the literature is seen to be quite good. The results obtained in this investigation at temperatures below the melting point of Cd agree favorably with those tabulated by Kubaschewski and Evans (1958, p. 32 8) but are somewhat lower than the values tabulated by Elliot and Gleiser (1960, p. 29-30).**

**In the experiments performed in this investigation at temperatures below the melting point of Cd, a tarnish of CdO was formed on the surface of the samples, This thin oxide film can reduce the value of the apparent vapor pressure in either or both of two ways : 1) by providing a barrier to the sublimation of Cd from the surface of the sample; and, 2) by adding oxygen to the sample, thereby reducing the observed weight loss. No oxidation was**



Figure 15. Variation of log P<sub>Cd</sub> above Pure Cd with **Reciprocal Temperature**

**observed in any of the other experiments.**

**In view of the fairly good agreement between the vapor pressure of Cd as determined in this investigation and the results found in the literature, it was decided that the apparatus and experimental technique used in this investigation provided for sufficiently accurate vapor-pressure measurement.**

## Vapor Pressure of  $Sb^2_2O_3$  in the Range from  $422^O$  to  $599^OC$

**The vapor-pressure studies performed on PbO-based slags, to be discussed later in this section, require that the vapor pressure of**  $\text{Sh}_{4}0^{\text{c}}$  **above pure**  $\text{Sh}_{2}0^{\text{c}}$  **be accurately known before the experimental data can be converted into** activities. Very few Sb<sub>4</sub>0<sub>6</sub> vapor-pressure data have been **reported in the published literature. Hineke (19 30, p. 2869) using a modified version of the inert gas saturation** method, has determined the vapor pressure of Sb<sub>4</sub>0<sub>6</sub> above cubic, orthorhombic, and liquid Sb<sub>203</sub> in the temperature **range from 4 70° to 800°C. Myzenkov and Klushin (1965, p. 1709), using the boiling-point method, have determined the** vapor pressure of  $\text{Sb}_{4}$ <sup>0</sup>  $_6$  above liquid  $\text{Sb}_{2}$ <sup>0</sup> $_3$  in the tempera**ture range from 715° to 1025°C.**

**The two investigations mentioned above show a large** discrepancy between the data for liquid  $\text{Sb}_2\text{O}_3$ . In the **investigation by Hincke, silica crucibles were used to con**tain the Sb<sub>2</sub>0<sub>3</sub>, whereas Myzenkov and Klushin used pure

**alumina crucibles. At high temperatures, above the melting** point of Sb<sub>2</sub>0<sub>3</sub>, it is to be expected that Sb<sub>2</sub>0<sub>3</sub> would dissolve SiO<sub>2</sub> from the crucibles with a resultant lowering of the vapor pressure of  $Sb^0$ <sub>6</sub>. This increased lowering of **the vapor pressure with temperature is seen as an increas**ing degree of curvature in the plot of  $p_{\text{Sb}_40_6}$  vs  $\frac{1}{\text{T}}$  shown **in Figure 16. Also included in Figure 16 are the results of Myzenkov and Klushin. Since the data of Hincke for liquid ^ 2^3 are somewhat doubtful, it was decided to use the data of Myzenkov and Klushin to refer the slag vapor-pressure data determined in this investigation to pure liquid** Their data for the vapor pressure above pure, liquid  $Sb_2^0$ <sup>3</sup> **in the temperature range from 656° to 10 25°C are represented by the formula :**

$$
\log P_{\text{Sb}_40_{6}} \quad \text{mm Hg} = 5.775 - \frac{4341}{T} \tag{10}
$$

**The vapor-pressure data of Hincke are the only data** reported in the literature for solid  $Sb_20_3$ . Since there **is some question as to the accuracy of his data for liquid s^ 2^ 3 ' it was decided to redetermine the vapor pressure above cubic Sb2Û3 in order to ascertain whether these data were in significant error.**

The Sb<sub>2</sub>0<sub>3</sub> was prepared for study by resubliming it in **argon at a temperature of 480°C, well below the cubicorthorhombic transition temperature of 5 70°C. The cubic**



Figure 16. Variation of log  $P_{Sb_40_6}$  above Liquid  $Sb_20_3$ with Reciprocal Temperature

**crystal modification of ^ thus produced was verified by x-ray diffraction analysis. The results of these experiments are shown in Figure 17 together with the data of Hincke. It is apparent from the figure that no errors have been introduced by using silica crucibles at temperatures** below the melting point of  $Sb_00_3$ . Hincke's data are some**what high because of his extrapolation of weight-loss versus flow-rate data to zero flow rate.**

**A linear regression analysis of the vapor-pressure data** for cubic  $Sb_2 0_3$ , as determined in this investigation, has **been made with the result that,**

$$
\log P_{\text{Sb}_40_{6}} \text{mn Hg} = 12.239 - \frac{10.441}{T} \tag{11}
$$

**heat of vaporization calculated from Equation (11) is given in Table 10 together with the values given in the literature for the temperature range from 422° to 599°C. The molar**

Crystal modification	$\Delta H$ , cal	Source	
cubic	47,780±1,330	This investigation	
cubic	47,320	Hincke	
orthorhombic	44,080	Hincke	
liquid	17,830	Hincke	
liquid	19,430	Myzenkov and Klushin	

Table 10. Heats of Sublimation and Vaporization of Sb<sub>4</sub>0<sub>6</sub>



**Figure 17. Comparison of Data for log P Sb406 above Cubic**  $Sb<sub>2</sub>0<sub>3</sub>$  as a Function of Reciprocal Temperature

## **Evaluation of Vapor-Pressure Data for the Determination of Thermodynamic Data for PbO-Si^C^ and PbO-SiC^-SL^O3 Slags**

## **at 700qC**

**The vapor-pressure data obtained in this investigation** can be used to calculate the thermodynamic activity of Sb<sub>2</sub>0<sub>3</sub> **in the two slag systems studied. By means of a Gibbs-Duhem integration, the thermodynamic activity of PbO can be** obtained for the Pb0-Sb<sub>2</sub>0<sub>3</sub> slags at 700<sup>o</sup>C. No further cal**culation of activities can be made for the PbO-SiO^-Sb^O3** slags since only the activity of Sb<sub>2</sub>0<sub>3</sub> was determined in **this investigation.**

Determination of Thermodynamic Data for Pb0-Sb<sub>2</sub>0<sub>3</sub> Slags at 700°C. The vapor-pressure determinations for the Pb0-Sb<sub>2</sub>0<sub>3</sub> system at 700°C made in this investigation are given in Table 3. Using the pressure above pure liquid  $Sb_20_3$  as 20.59 mm Hg, as determined by Myzenkov and Klushin (1965, p. 1715), the individual activities of  $\text{Sb}_{2}$ <sup>0</sup> a have been cal**culated. The results of these calculations are shown in Table 11. Maier and Hincke (19 32, p. 3-12) have made a limited number of vapor-pressure measurements in the PbO-** $Sb_20_3$  system at  $697^{\circ}$ C using the inert gas saturation method. Their measurements were converted to Sb<sub>2</sub>0<sub>3</sub> activities using **the somewhat low value of 13.0 mm Hg for the pressure above pure Sb2& 3, as determined by Hincke (1930, p. 3876). A**

**recalculation of their data using 20 6 59 mra\* Hg rather than** 13.0 mm Hg as the pressure above pure  $\text{Sb}_{2}\text{O}_{3}$  is included in **Table 11 for comparative purposes. All activities are** relative to pure, liquid  $Sb_2^0$  at the respective temperature. **It is evident that the agreement is rather poor at low con**centrations of Sb<sub>2</sub>0<sub>3</sub> although their data are not extensive **enough for an accurate comparison to be made.**

Table 11. Activities of Sb<sub>2</sub>0<sub>3</sub> in the Pb0-Sb<sub>2</sub>0<sub>3</sub> System **Determined from Vapor-Pressure Measurements in** the  $Pb0-Sb_203$  System at  $700^{\circ}C$ 

$T_{\rm G_C}^{\rm emp}$ ,	$x_{Sb_20_3}$	$a_{\text{Sb}_20}$	$\gamma_{\text{Sb}_20}$	Source
700	0.0442	0.0385	0.871	This investigation
700	0.108	0.0377	0.349	$\mathbf{B}$ Ħ
700	0.137	0.0375	0,274	$\mathbf{u}$ n
697	0.144	0.0624	0.433	Maier and Hincke
700	0.176	0.0430	0.244	This investigation
700	0.212	0.0522	0.246	$\mathbf{u}$ $\cdot$ H
700	0.280	0.0782	0.279	$\mathbf{u}$ $\mathbf{u}$
700	0.495	0.245	0.495	$\mathbf{u}$ n
697	0.503	0.222	0.441	Maier and Hincke
697	0.730	0.630	0.863	Ħ $\mathbf{u}$

**The somewhat peculiar behavior observed for the twocomponent mixtures containing 4.42, 10.8, and 13.7 mole %** Sb<sub>2</sub>0<sub>3</sub> is due to the fact that these compositions lie

**within a two-phase region composed of solid PbO and liquid** containing 14.4 mole % Sb<sub>2</sub>0<sub>3</sub>. The locations of these **compositions relative to the phase boundaries are shown in** the phase diagram for the PbO-Sb<sub>2</sub>O<sub>3</sub> system presented in **Figure 18, Zunkel and Larson (1967, p. 477). Since the "composition of the liquid in the two-phase region is constant, the individual component activities remain equal between the solidus and liquidus compositions.**

**A Gibbs-Duhem integration of the activity data obtained in this investigation has been used to obtain the activities of** Pb0 in the range from  $X_{Pb0} = 0.959$  to  $X_{Pb0} = 0.505$  at **700°C. The data for this calculation are given in Table 12.** A plot of the  $\alpha$ -function for  $Sb_20_3$  as a function of mole fraction of  $Sb_2O_3$  is presented in Figure 19. Since  $\alpha$  is **not constant or linear as a function of composition, the** Pb0-Sb<sub>2</sub>0<sub>3</sub> system is neither regular nor sub-regular in its **behavior at 700°C. It is also readily apparent from Figure 19 that this system is far from being ideal due to the strong negative deviation observed.**

The activities of Sb<sub>2</sub>0<sub>3</sub> calculated from the vapor**pressure determinations in the PbO-Sb^O^ system and the activities of PbO calculated by means of the Gibbs-Duhem integration are shown graphically in Figure 20. The** standard states are the real, pure liquid for  $\text{Sb}_2^0$  and **the real, pure solid for PbO, both at 700°C. It can be**

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**Figure 18. Phase Diagram for the PbO-rich End of the** Pb0-Sb<sub>2</sub><sup>0</sup><sub>3</sub> System

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Figure 19. Variation of the  $\text{Sb}_2^0$  a-function with Composition for the PbO-Sb<sub>2</sub>0<sub>3</sub> System at 700<sup>o</sup>C



Figure 20. Activities of  $Sb_20_3$  and PbO in the PbO-Sb<sub>2</sub>0<sub>3</sub> System at 700°C (standard states: Sb<sub>2</sub>0<sub>3</sub>-pure **liquid, PbO-pure solid)**





 $\ast$ 

 $x_{PDO}^2$  $ln \frac{1}{2}$  $\mathbf{u}$  $\alpha_{\text{Sb}_2 0_3} = \frac{1 \text{m}_{\text{Sb}_2 0_3}}{(1 - x_{\text{Sb}_2 0_3})^2}$  seen that the behavior of  $Sb_20_3$  deviates strongly in **the negative direction from ideality and appears to remain** so at all compositions. The behavior of Pb0, however, **presents a rather interesting case which can be explained by considering the integrated form of the Gibbs-Duhem equation for a binary system:**

$$
ln\gamma_1 = -\int_{x_1}^{x_1} = \frac{x_1}{x_1} \frac{x_2}{d(ln\gamma_2)}
$$
 (12)

If  $\gamma_2$  continually increases as  $X_2$  decreases, then  $\gamma_1$  is greater than unity at all values of  $X_2$ . Also, if  $\gamma_2$  continually decreases as  $x_2$  decreases, then  $y_1$  is less than unity at all values of  $X_2$ . In the first case, component **1 exhibits positive deviation from the Raoult's law line over the entire composition range and in the second case, component 1 exhibits negative deviation from the Raoult fs** law line over the entire composition range. Close examination of the data of Table 12 reveals that  $\frac{\gamma_{\text{Sb}_2 0}}{2}$ , although **it is much less than unity at all compositions studied, does not continually decrease as**  $^{X}$ **Sb<sub>2</sub>0<sub>3</sub> decreases. As the composition of the system enters the two-phase region (see** Figure 18) where  ${}^{a}Sb_{2}0_{3}$  becomes constant with composition, Ysb<sub>2</sub>0<sub>3</sub> must of necessity begin to increase as the concentration of  $\text{Sb}_2^0$  continues to decrease. Thus, the fact that  $\frac{\gamma_{\text{Sb}_2^0}}{3}$  is always less than unity is not sufficient to

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**insure that PbO also continually deviates in the negative** direction from Raoult's law line. This unusual mixed **behavior is also seen to occur in some silicate systems DeWitt and Seitz (1939/ p. 3170)• as well as some metallic systems, e.g. Zn-Sb at 550°C**

The standard free energy of formation of liquid Sb<sub>2</sub>0<sub>3</sub> has been estimated by Coughlin (1954, p. 8) using heat **capacity data for the orthorhombic crystal modification of** solid  $\text{Sb}_2\text{0}_3$ . By proper treatment of the  $\text{Sb}_2\text{0}_3$  activity data **determined in this investigation, together with the slagmetal equilibria data for the PbO~Bb^O^ system reported by** Zunkel and Larson (1967, p. 475), a calculation can be made for the standard free energy of formation of  $Sb_20_3$  as a **function of temperature. The equilibria reaction under consideration can be represented as follows :**

$$
2 S_{\text{b}_{10}t\text{m}} + 3 P_{\text{b}_{0}}(1) = S_{\text{b}_{2}0} (1) + 3 P_{\text{b}_{1}}(1) \tag{13}
$$

**The equilibrium constant for this reaction is represented by the following expression:**

$$
K_{eq} = \frac{a_{Pb}^{3} \times a_{Sb}^{20} - 3}{a_{Pb0}^{3} \times a_{Sb}^{2}}
$$
 (14)

**Several assumptions can be made to simplify this expression : 1) that Henry's law is obeyed over a sufficiently wide range of both temperature and concentration for Sb dissolved in** Pb, 2) that  $\Delta$ Cp for the reaction is zero, 3) that  $a_{\text{phn}}$  is

unity, and 4) that  $Sb_2O_A$  and  $Sb_2O_B$  may be present in small **amounts but do not affect the equilibrium. Assumption 1 is valid because Sb dissolved in Pb follows Henry's law up to approximately 3.9 wt % in the temperature range under consideration. Assumption 2 is valid because AH° and AS° are nearly independent of temperature in the range under consideration. Assumption 3 is valid since all alloys under consideration contain in excess of 99 wt % of Pb. Assumption 4 can be shown to be valid by application of the appropriate data from Table 13. As an example, if the oxygen potential in the system is assumed to be determined** by the  $2 \text{ Pb0}$   $(1) = 2 \text{ Pb} (1) + 02(q)$  equilibrium,  $a_{Sb_20_4}/a_{Sb_20_3} = 2.7 \times 10^{-3}$  and  $a_{Sb_20_5}/a_{Sb_20_4} = 1.5 \times 10^{-9}$ **at 700°C.**

**Using the above assumptions. Equation (14) reduces to:**

$$
K_{eq} = \frac{a_{Sb}^2 O_3}{\frac{3}{a_{Pb0}^2 (8 \text{ SD})^2}}
$$
 (15)

Zunkel and Larson (1967, p. 476) have shown that  ${\rm {}^{a}Sb} _{2} {\rm 0}_{3} / {\rm a}_{\rm Ph0} ^{\rm 3}$ **is a constant independent of temperature in the two-phase** region in the PbO-rich end of the PbO-Sb<sub>2</sub>0<sub>3</sub> system. There-**YSb203 fore, in the two-phase region, a plot of log — — versus xSb203 YPbO log — ~— — should be a temperature-independent straight**  $\mathbf{r}_{\text{Pb}0}$ **line with a slope of - 1 .**

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The data for constructing the  $\log \frac{\gamma_{\text{Sb}_20_3}}{\sqrt{3}}$  versus **log — — -— plot are given in Table 14 and the plot itself**  $x_{\text{Sb}_2 0}$ **is shown in Figure 21. The data for 650° and 750°C were** plotted using the assumption that  $a_{Pb0} = 0.96$ , since **insufficient data were collected to perform a Gibbs-Duhem integration for these temperatures with any degree of accuracy. Also included in Figure 21 are the slag-metal equilibria data of Zunkel and Larson plotted using the estimated values for the standard free energy of formation** of  $Sb_2^0$  according to Coughlin. As can be seen from **Figure 21, the data fall on a temperature-independent straight line with a slope of -1 for all compositions within the two-phase region. The intercept of this line has been calculated with the result that,**

$$
\frac{a_{\rm Sb_20_3}}{a_{\rm Pb0}^3} = 0.0430\tag{16}
$$

**for the two-phase region**

**Using the data of Zunkel and Larson,**

$$
\log\left(\frac{2}{3}\right)\frac{\text{S}}{\text{D}}\big)^2 = -\frac{4980}{T} + 2.798\tag{17}
$$

**and Equations (15) and (16), a linear equation in tempera**ture for the variation of log K<sub>eq</sub> with temperature can be **obtained with the result that,**



\* apbo estimated (see p. 88)



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$$
\log K_{\text{eq}} = \frac{4980}{T} - 4.165 \tag{18}
$$

**for Reaction (13).**

**The appropriate data from Table 13, together with Equation (18) can then be used to calculate the standard** free energy of formation of  $Sb_2 0 \cdot 1$  according to the **following reaction :**

$$
2 Sb_{(1)} + \frac{3}{2} 0_{2(g)} = Sb_{2} 0_{3(1)}
$$
 (19)

**with the result that,**

$$
\Delta G_{\rm f}^{\rm O} = -159,190 + 56.20 \text{ T} \tag{20}
$$

**Equation (20) was obtained from a least-squares fit of three values of**  $\Delta G^{\circ}_{f}$  **calculated at 650°, 700°, and 750°C.** These **values are compared with the estimated values of Coughlin** in Table 15. Although the correction in  $\Delta G_{f}^{O}$  for  $\mathrm{Sb}_{2}0_{3}$ **amounts to less than 3 percent, the estimated data for**

$$
\log \frac{a_{\text{Sb}_2 0}}{a_{\text{Pb}_0}}
$$
 are in error by approximately one-half order of mag-

**nutide. It is to be noted, however, that the application of Figure 21 to the determination of the liquidus and solidus** curves in the PbO-rich end of the PbO-Sb<sub>2</sub>0<sub>3</sub> system, as was **done by Zunkel and Larson, is not affected by the correc**tion in  $\Delta G_{f}^{O}$  for  $\text{Sb}_{2}^{O}$ <sub>3(1)</sub>, since the curves are shifted only **in the vertical direction.**

Table 15.  $\Delta G^O_f$  for  $Sb_2O_{3(1)}$  as Determined from Slag-Metal Equilibria Data in the Pb-(Pb0+Sb<sub>2</sub>0<sub>3</sub>) System **and Vapor-Pressure Determinations in the** Pb0-Sb<sub>2</sub>0<sub>3</sub> System at  $650^{\circ}$ , 700<sup>o</sup>, and 750<sup>o</sup>C

Temperature, <sup>O</sup> C	$\Delta G_{f}^{O}$ , cal (This study)	$\Delta G_{f}^{O}$ , cal (Coughlin)
650	$-107,320$	$-109,410$
700	$-104,490$	$-106,710$
750	$-101,700$	$-104,010$

**The data of Table 14 can also be used to calculate the** heat of vaporization of Sb<sub>4</sub>0<sub>6</sub> from artificial slags whose **compositions fall within the two-phase region in the PbO**rich end of the Pb0-Sb<sub>2</sub>0<sub>3</sub> system as shown in Figure 18. By means of a plot of log  $P_{\text{Sb}_40}$  versus  $\frac{1}{p}$  over the temperature **range from 650° to 750°C, a value of +20,830 cal/rnole has been calculated. This value is seen to be somewhat larger** than the corresponding value for  $\Delta H_{\text{vap}}$  of pure  $Sb_2^0$  due to the strong negative deviation of Sb<sub>2</sub>0<sub>3</sub> from the Raoult's **law line as shown in Figure 20.**

The phase diagram for the PbO-Sb<sub>2</sub>O<sub>3</sub> system shown in **Figure 18 may be used to calculate the standard free energy of formation of PbO'Bb^O^. At a temperature just below the eutectic temperature, the following reaction may be considered :**
$$
\frac{\text{Pb0}}{\text{(a)}}\text{(a)} + \frac{\text{Sb}_2\text{0}_3}{\text{20}_3\text{(a)}} = \text{Pb0} \cdot \text{Sb}_2\text{0}_3\text{(s)}
$$
 (21)

**The equilibrium constant for this reaction is represented by the following expression :**

$$
K_{eq} = \frac{a_{Pb0} \cdot sb_2 0_3}{a_{Pb0} \cdot x \cdot a_{Sb_2 0_3}}
$$
 (22)

The activity of  $Pb0 \cdot Sb_20_3$ , referred to the pure solid, can **be set equal to unity using the pure solid as the standard state. For purposes of calculation, the activity of PbO can be set equal to its mole fraction; 0.9 44 at 60 4°C. The** activity of  $\text{Sb}_2\text{O}_3$  can be obtained from the data given in Table 14 for the 2-phase slag compositions. By extrapolating log  $p_{Sb_40_6}$  versus  $\frac{1}{T}$  to 604°C and dividing the resultant **pressure by**  $p_{Sb_40_6}^{\circ}$  **= 2.203 nun Hg at 604°C (Hincke, 1930, p. 3876),**  $a_{Sb_20}$  **is calculated to be 0.0647, relative to** pure, solid  $\text{Sb}_2\text{O}_3$ .

**Substitution of the above values into equation (22) at**  $604^{\circ}$ C yields K<sub>eq</sub> =16.4 for the reaction:

$$
Pb0 (s) + Sb203 (s) = Pb0 \cdot Sb203 (s)
$$
 (23)

**By use of the relation,**

$$
\Delta G^{\mathbf{O}} = -RT \ln K_{\mathbf{eq}} \tag{24}
$$

**the standard free energy change for reaction (23) can be** calculated with the result that  $\Delta G^{\circ}_{877} = -4,860$  cal/mole of Pb0 $\cdot$ Sb<sub>2</sub>0<sub>3</sub>.

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 $\bullet$ 

The standard free energy of formation of  $Pb0 \cdot Sb_2 0_3$  from **the elements at 6040C can be calculated by summing the following equilibria and their corresponding free energy values.**

 $\bullet$ 

\n
$$
P_{00}(s) + S_{02}O_{3}(s) = P_{00}S_{02}O_{3}(s)
$$
\n

\n\n
$$
AG_{877}^O = -4,860 \text{ cal}
$$
\n

\n\n
$$
G_{877}^O = -740 \text{ cal}
$$
\n

\n\n
$$
SG_{877}^O = -740 \text{ cal}
$$
\n

\n\n
$$
G_{877}^O = -740 \text{ cal}
$$
\n

\n\n
$$
G_{877}^O = -740 \text{ cal}
$$
\n

\n\n
$$
2S_{01}(1) + \frac{3}{2}O_{2}(g) = S_{02}O_{3}(1)
$$
\n

\n\n
$$
AG_{877}^O = -109,900 \text{ cal}
$$
\n

\n\n
$$
G_{877}^O = -109,900 \text{ cal}
$$
\n

\n\n
$$
P_{01}(1) + \frac{1}{2}O_{2}(g) = P_{00}(s)
$$
\n

\n\n
$$
G_{877}^O = -31,080 \text{ cal}
$$
\n

\n\n
$$
G_{877}^O = -31,080 \text{ cal}
$$
\n

\n\n
$$
G_{877}^O = -31,080 \text{ cal}
$$
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G_{877}^O = -31,080 \text{ cal}
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G_{877}^O = -31,080 \text{ cal}
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G_{877}^O = -31,080 \text{ cal}
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G_{877}^O = -31,080 \text{ cal}
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$$
G_{877}^O = -31,080 \text{ cal}
$$
\n

\n\n
$$
G_{877}^O = -31,080 \text{ cal}
$$
\n

\n\n
$$
G_{877}^O = -31,080 \text{ cal}
$$
\n

\n

$$
Pb_{(1)} + 2Sb_{(1)} + 20_{2(g)} = Pb0 \cdot Sb_{2}0_{3(s)}
$$
  

$$
\Delta G_{877}^{O} = -146,580 \text{ cal}
$$
 (29)

**The literature does not contain any data with which this calculated value can be compared.**

Determination of Thermodynamic Data for Pb0-SiO<sub>2</sub>-Sb<sub>2</sub>0<sub>3</sub> **Slags at 70Q°C. The vapor-pressure determinations for the**  $Pb0-Si0^2-Sb^20^3$  slags have been converted to  $Sb^20^3$  activities using the data of Table 4 by means of  $p_{Sb_A0_G}^{\bullet} = 20.59$  ram Hg **at 700°C, as determined by Myzenkov and Klushin. The results of these calculations are presented in tabular form in Table 16 and shown graphically in Figure 22. The molar ratio of** Pb0 to Si0<sub>2</sub>, for reasons to be explained later in this **chapter, was held constant at a value of 2 for all slag compositions studied in this investigation.**

Table 16. Activities of  $Sb_2 0_3$  in the Pb0-Si0<sub>2</sub>-Sb<sub>2</sub>0<sub>3</sub> System  $(\frac{Pb0}{S10} = 2)$  Determined from Vapor-Pressure Measurements in the  $Pb0-Si0_{2}-Sb_{2}0_{3}$  System at 700<sup>°</sup>C  $x_{Sb_20}$ <sub>3</sub>  $x_{Sb_20}$ <sub>3</sub>  $x_{Sb_20}$ <sub>3</sub>  $x_{Sb_20}$ <sub>3</sub> **0.0296 0.00511 0.173 0.0634 0. 0116 0.183. 0.0945 0.0193 0.204 0.130 0.0359 0.276** 

**0.167 0.0625 0.374 0.206 0.0995 0.483**

**0.246 0.146 0.593**



**PbO Figure 22.** Activity of  $\text{Sb}_{2}\text{O}_{3}$  in PbO-SiO<sub>2</sub>-Sb<sub>2</sub>O<sub>3</sub> ( $\frac{1}{\text{S10}}$  = 2) **Slags at 7O0°C (Standard state - pure liquid Sb2 0^)**

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**No calculation can be made for the component activities of PbO and SiO^ in the slags studied in this investigation,** since only the activity of Sb<sub>2</sub>0<sub>3</sub> was determined experimental**ly. Some outside data source would be required before a ternary Gibbs-Duhem integration could be performed. Sridhar and Jeffes (1967, p. 44) have determined the activities of both PbO and SiO^ in the PbO-SiO^ system up to the limit of silica saturation at 850°, 950°, and 1050°C, and have compared their results with those of earlier workers. In all cases, it was found that both PbO and ^iO^ exhibit strong** negative deviations from the Raoult's law line at compositions below approximately  $X_{S102} = 0.5$ . For compositions **containing higher silica contents, silica begins to deviate positively from the ideal Raoult1s law line and continues to do so up to the saturation limit. The negative deviation shown for PbO is to be expected due to the strong tendency for PbO to form silicates.**

For comparative purposes, the vapor-pressure data for **i 2** both the PbO-SiO<sub>2</sub>-Sb<sub>2</sub>O<sub>3</sub> ( $\frac{200}{3000}$  = 2) slags and the PbO-Sb<sub>2</sub>O<sub>3</sub> slags are plotted together as a function of  $X_{Sb_20_3}$  at  $700^{\circ}C$ in Figure 23. At low concentrations of Sb<sub>2</sub>0<sub>3</sub>, the vapor **pressure of Sb** $_40^{\circ}$  is highest above the binary slags. At higher concentrations, above approximately  $X_{Sb203} = 0.21$ , the vapor pressure of  $Sb_40^c_6$  is highest above the ternary silicate slags (on PbO+Sb<sub>2</sub>O<sub>3</sub> basis). A continuous decrease

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**Figure 23. Variation of log ^Sb^O^ with Composition for**  $Pb0-Si0_{2}-Sb_{2}0_{3}$  ( $\frac{200}{272}=2$ ) and  $Pb0-Sb_{2}0_{3}$  Slags **at 700°C 2**

of  $P_{\text{Sb}_A 0_A}$  with decreasing concentration of  $\text{Sb}_2 0_{3}$  in the slag **is observed for the silicate slags due to the fact that they are composed entirely of liquid over the composition range investigated in this study at 700°C. Further discussion of the shapes of the curves of Figure 23 and their relationship to one another will be deferred until later in this chapter.**

## **Application of Vacuum Techniques to the Removal of AS2Og , Sb2Û g, and SnO2 from Lead-Softening Slags**

**The primary purpose of this investigation is to determine the feasibility of removing volatile oxide impurities from the PbO-based slags produced during the softening of lead bullion by the application of vacuum techniques. Current softening practice involves a selective oxidation pro**cess in which a suitable oxidizing agent, air or Pb0, is **added to the lead bullion to oxidize the impurities which then dissolve in a slag composed primarily of PbO. The slag phase produced in this operation must then be recovered and separately treated to recover the oxides of the impurity metals. After reverberatory softening operations, the impurity metal oxides are recovered by fuming the slag in the presence of carbon to produce an antimonial-Pb and a fume composed primarily of the trivalent oxides of As and Sb. In kettle softening, sodium salts are added together with PbO to produce a nonvolatile liquid solution of sodium**

**arsenates, antimonates, and stannates which require further treatment to recover the impurity metals either as pure oxides or metals.**

**The results of this study propose that, provided the** concentration of  $Sb_20$ <sub>3</sub> in the slag is sufficiently high, slag treatment for the recovery of Sb as the trivalent oxide **can be greatly simplified while, at the same time, producing a high purity product of Sb.**

**The experiments performed in this portion of the investigation were concerned primarily with the relative rates at which the oxides of As, Sb, and Sn could be removed from slag melts under conditions of elevated temperature and reduced pressure. This experimental investigation is intended as a feasibility study rather than a rigorous kinetic study of the various steps occurring in the overall process. A great deal of further work, not included in this study, would have to be done before any quantitative statements could be made concerning the actual rates of removal or the mechanisms by which the actual removal is effected. In view of this stated purpose, the operating variables including temperature, pressure, slag composition, and addition agents were modified in an attempt to determine the optimum conditions for the removal of volatile oxides from lead-softening slags. The vacuum-removal experiments performed in this portion of the investigation can be conveniently divided into two**

**separate categories: 1) those without silica additions ; and, 2) those with silica additions. Each group of experiments will be discussed separately in the following sections. All x-ray diffraction phase analyses for the slags and condensates produced are presented in Table 9.**

The Removal of  $\text{As}_2\text{O}_3$ ,  $\text{Sb}_2\text{O}_3$ , and  $\text{SnO}_2$  from  $\text{Pb0-Me}_x\text{O}_y$ **Slags at Reduced Pressure and Elevated Temperature. The** experimental data for the removal of  $\text{As}_20_3$ ,  $\text{Sb}_20_3$ , and  $\text{Sn0}_2$ **from Pb0-Mex0y slags are given in Taoie 6 and presented in graphical form in Figures 2 4-28. With the exception of test G, all tests were made at a reduced pressure of 200p Hg; test G being made at atmospheric pressure,**

**The first tests that were run (H and J) were made to determine the feasibility of selectively dis tilling As^O^** from a 2 wt %  $As_2O_3-Pb0$  slag at 500<sup>°</sup> and 650<sup>°</sup>C under a **vacuum of 200p Hg. Both slags used for these tests were first preformed, cooled, and crushed to -150 mesh before** being used for the tests. In test H, the As<sub>2</sub>0<sub>3</sub> content was **reduced from an initial concentration of 1,80 wt % to a value of 1.32 wt % in a 4-hr period under a vacuum of 200y Hg at 500°C. By increasing the temperature to 650°C, as in** test J, the residual amount of  $As_{2}0_{3}$  was reduced to 0.96 **wt %, approximately one-half of the original amount. Due to** the very high vapor pressure of As<sub>2</sub>0<sub>3</sub>, no measurable amount **of condensate was produced in either of these tests. A**

**noticeable deposit was observed, however, on the inside walls of the vacuum take-off line and trap and it was noticed that the vacuum pump oil became cloudy during both tes ts.**

**Because As usually comprises only a small fraction of the impurity oxides in commercial lead softening slags, no further extensive program of experimentation was carried out** to investigate the removal of  $As_20<sub>3</sub>$  from binary  $As_20<sub>3</sub>-Pb0$ slags, except for a third test made at 800°C. The results **of this test (DD) are presented in Figure 24 and given in tabular form in Table 6. It is apparent that the vacuum** distillation of  $As^0_2O^3_3$  from this slag at 800<sup>°</sup>C is no more **efficient than that observed for test J . The primary reason for this behaviour is due to the drastic decrease in available surface area of the slag. The enhanced volatility of As^Og at the higher temperature has been nullified by virtue of the fact that the slag no longer has a high specific surface and, in addition, is composed of a very viscous, 2-phase mixture which is very difficult to stir effectively.**

**The second series of tests conducted in this portion of the investigation were made to determine the feasibility of** selectively distilling  $\text{Sb}_{2}0^{\circ}$  from binary PbO-Sb<sub>2</sub>0<sub>3</sub> slags at **reduced pressure over a wide variety of temperatures. Since** the majority of lead softening slags contain  $\text{Sb}_2\text{O}_3$  as the **major oxide impurity, there is considerably more justification**



**Figure 24. Removal of As from a 3 wt % AS20^-PbO Slag by Vacuum Distillation at 800°C: Test DD, 200y Hg Pressure.**

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**in investigating these binary slags than there is in the case of As,**

**Before any tests were made at reduced pressure, one test (G) was made at atmospheric pressure at 750°C to determine whether Sb^O^ could be removed from a slag without the necessity of applying a vacuum. The results of test G are included in Figure 25 and clearly indicate that no substantial reduction in the Sb content of the slag took place. Approximately 2 gm of condensate were recovered which con**tained 74.87 wt  $\frac{1}{6}$  of  $Sb_20_3$  and 22.37 wt  $\frac{1}{6}$  Pb0.

**The results of a series of tests made under reduced pressure at 650° and 750°C are given in Table 6 and included in Figure 25, In test E, made at 650°C, approximately 30% of the Sb was removed from the slag over a 4-hr period. Very little condensate was recovered, however, which may have been due to the nucléation of solid particles of**  $Sb^0$ <sup>2</sup> in the gas phase which were swept out of the reaction **tube by the vacuum pump. The condensate which was recovered** contained  $92.29$  wt  $%$  Sb<sub>2</sub>0<sub>3</sub> and 4.42 wt  $%$  Pb0, which is a **considerable improvement in grade over the previous test ( G) .**

**The remaining two tests made at 750°C (F and AA) differ only in duration. By increasing the time from 4 hr (test F)** to 12 hr (test AA), a further small reduction in the  $Sb_2O_3$ **content of the slag was achieved with a corresponding**

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Figure 25. Removal of Sb from a 30 wt % Sb<sub>2</sub>0<sub>3</sub>-Pb0 Slag by **Vacuum Distillation at 650° and 750°C**

**increase in the yield of condensate. Both condensates pro**duced contained in excess of 95 wt % Sb<sub>2</sub>0<sub>3</sub>.

The results of a second series of tests (II, IH, JJ, BB, and GG) made on Sb<sub>2</sub>0<sub>3</sub>-Pb0 slags are given in Table 6 and **shown graphically in Figures 26 and 27. The results of test II, made at 700°C/ and tests HH and JJ, made at 775°C, offer little more than what has been learned from the tests already described. It is apparent that as the temperature** is raised the removal of  $Sb_2^0$  becomes increasingly more efficient because of the increased vapor pressure of  $\mathrm{Sb_{4}0_{6}}$ **and. the decreased viscosity of the slags, which provides for more effective stirring of the melt. The analyses of the condensates produced in these tests, given in Table 6 , appear to be somewhat uncertain due to the fact that they** begin to show in excess of 100 wt  $8$  Sb<sub>2</sub>0<sub>3</sub>. By assuming **that the PbO analyses are somewhat more reliable, however,** the condensates appear to contain at least 98 wt % Sb<sub>2</sub>0<sub>3</sub>.

**The disadvantage of operating at higher temperatures is shown by the results of tests BB and GG which were made at a temperature of 850°C. The results of these tests are given in Table 6 and shown graphically in Figure 26.** The increased volatility of Sb<sub>4</sub>0<sub>6</sub> together with the decreased **slag viscosity result in more efficient removal of Sb from the slag but the higher temperature also allows for the increased volatility of PbO. In both tests the recovery of**



**Figure 26. Removal of Sb from a 30 wt % Sb^O^~RbO Slag by Vacuum Distillation at 700° and 850°C**

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**Figure 2 7. Removal of Sb from a 30 wt % SbgiO^-PbO Slag by Vacuum Distillation at 775°C**

**Sb as the trioxide was found to be greater than 70 wt %.** The purity of the condensates produced was, however, quite a bit lower than that for tests II, HH, and JJ. The **increased vapor pressure of PbO at this temperature accounted for approximately 6 wt % PbO in the condensates.**

**A third series of tests made on PbO-Sb^O^ slags was carried out at 700°C without first preforming the slags at a higher temperature to insure a completely liquid melt at the beginning of the tests. The slags used for tests LL and MM were preformed, cooled, and ground to 90%-65 mesh. In** test LL the removal of  $Sb^0$ <sup> was approximately the same as</sup> **that observed for test II, in which the slag was initially super-heated. The surface of the particles of slag used for** this test were depleted in Sb<sub>2</sub>0<sub>3</sub> during the heating-up period **and prevented their coalescing into one mass. Some sintering was observed at the end of the test but the slag remained rather loosely granular. Test MM essentially duplicated test LL except that the initial Sb content of the slag was reduced to 22 wt %, approximately the composition of the slag at the end of test LL. Practically no further reduction in the Sb content of the slag was achieved in this test. Test NN was also essentially a duplication of test LL with the exception that the preformed slag was ground to 90 % -150 mesh. The Sb content of the slag** decreased from 26.95 wt %  $Sb_2^0$ <sub>3</sub> initially to 7.40 wt %  $Sb_2^0$ <sub>3</sub>

**at the end of the 8-hr period. The much reduced particle size resulting in an even greater increase in the specific surface was responsible for the very low level to which Sb was removed from the slag. The condensates produced** in tests LL and NN contained above 98 wt  $8$   $Sb<sub>2</sub>0<sub>3</sub>$ . The con**densate produced in test MM showed a somewhat lower Sb** content due to the small amount of removal of  $\text{Sb}_2\text{O}_3$ .

**One series of tests was made to determine the relative rates at which As and Sb could be removed from a 3 wt %**  $\text{As}_2\text{O}_3$ -30 wt %  $\text{Sb}_2\text{O}_3$ -PbO slag at 750<sup>°</sup> and 800<sup>°</sup>C under a **reduced pressure of 200p Hg. The results of these tests (P and CC) are given in Table 6 and shown graphically in Figure 2 8 . The removal of Sb from these slags compares with the results obtained in the previous tests made on the** binary slags. The removal of As, however, presents an **interesting phenomenon. In test P the removal of As just balances the reduction in the total slag volume caused by** the distillation of relatively large amounts of  $\text{Sh}_2\text{O}_3$ . As **a result, the concentration of As in the melt remains virtually constant. When the temperature is raised to o 800 C, for test CC, the increased rate of removal of Sb causes the residual concentration of As in the slag to actually increase during the test. The condensates produced in these two tests contained less than 2 wt % PbO and** almost equal amounts of  $\text{As}_2^0$ , 3.07 wt  $\text{R}^3$  for test P and

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Figure 28. Removal of As and Sb from a 3 wt % As<sub>2</sub>0<sub>3</sub>-30 wt % **Sb203--Pb0 Slag by Vacuum Distillation at 750° and 800°C**

**2.58 wt % for test CC.**

Since the vapor pressure of Sn0<sub>2</sub> is considerably less than that of either  $Sb_20_3$  or  $As_20_3$ , and since lead-softening slags seldom contain more than 10 wt % Sn0<sub>2</sub>, no comprehen**sive series of tests was made to investigate the vacuum** distillation of Sn0<sub>2</sub> from Sn0<sub>2</sub>-Pb0 slags. One test (U) was made on a 3 wt %  $As_{2}0_{3}-25$  wt %  $Sh_{2}0_{3}-12$  wt %  $Sn0_{2}-Pb0$ **slag under reduced pressure at 700°C. The results of this test are given in Table 6 . Neither of the three impurity oxides present was removed from the slag to any appreciable extent. Twenty-seven gms of condensate were recovered which** contained 95.28 wt % Sb<sub>2</sub>0<sub>3</sub>, 2.96 wt % As<sub>2</sub>0<sub>3</sub>, 2.34 wt % Sn0<sub>2</sub>, **and 0.99 wt % PbO.**

The vacuum-removal experiments briefly outlined above **were performed in an attempt to determine the feasibility** of removing  $As_2O_3$ ,  $Sh_2O_3$ , and  $SnO_2$ , at the concentrations at **which they normally occur in lead-softening slags. This procedure is not technically feasible under the conditions used in this investigation and, as a result, will not be considered further.**

The vacuum distillation of Sb<sub>2</sub>0<sub>3</sub> from lead-softening **slags appears to be much more favorable. Two main factors contribute to the potential application of vacuum techniques** to the removal of Sb<sub>203</sub>. Of primary importance is the fact that the vapor pressure of  $Sb^0$ <sub>6</sub> is very much higher than

**that of PbO. As a result, a near-perfect separation of** Sb<sub>2</sub>0<sub>3</sub> from PbO is at least theoretically possible. The **second factor, of perhaps more importance than the first, is that commercially-produced lead-softening slags normally** contain much higher concentrations of  $\text{Sb}_2\text{O}_3$  than of either  $\text{As}_2$ <sup>0</sup> 3 or Sn0<sub>2</sub>. This high concentration of Sb<sub>2</sub><sup>0</sup> 3 allows for **a sufficiently rapid rate of removal as to be of interest economically.**

**Several of the tests described above resulted in the** removal of approximately 75% of the original Sb<sub>2</sub>0<sub>3</sub> content **of the slag. The time required to achieve this result, however, is much too long to be of interest on a commercial scale. Therefore, before any set of optimum conditions for** the vacuum removal of Sb<sub>2</sub>0<sub>3</sub> from lead softening slags can **be formulated, it is necessary to reduce this time as much as possible.**

The Removal of  $\text{Sb}_2\text{O}_3$  from  $\text{Pb0-Si0}_2\text{-Sb}_2\text{O}_3$  Slags at **Reduced Pressure and Elevated Temperature. The rate of** removal of  $\text{Sb}_2\text{0}_3$  from lead-softening slags can be achieved **in either or both of two ways. The most obvious of these would be to conduct the tests at a lower reduced pressure. In doing so, however, the vaporization of PbO would also be increased which would result in an impure condensate being produced. A second alternative would be to determine suitable slag addition agents which would result in 1) an**

**increased activity, and hence an increased vapor pressure,** of Sb<sub>2</sub>0<sub>3</sub>, 2) a decreased activity, and hence a decreased **vapor pressure of PbO, and 3) a decreased slag viscosity, dither or all of these effects would result in an increased yield of higher purity bb^O3 condensate.**

**It was determined that the addition of silica to the** binary Pb0-Sb<sub>2</sub>0<sub>3</sub> slags studied in the previous section would **fulfill the second objective of a desirable addition agent, as discussed above. Lead oxide has a strong tendency to form silicates in the presence of silica at elevated tempera**tures. The phase diagram for the Pb0-Si0<sub>2</sub> system is shown **in Figure 29, It can be seen from Figure 29 that PbO forms at least 3 stable Pb-silicates at elevated temperatures ;**  $\beta$ -4Pb0·Si0<sub>2</sub>, 2Pb0·Si0<sub>2</sub>, and Pb0·Si0<sub>2</sub>. In addition, at **least one other Pb-silicate has been observed to occur in nature with a composition corresponding to 3PbO•2Si02• In order to determine the effect of silica additions to lead**softening slags on the rate of removal of Sb<sub>2</sub>0<sub>3</sub> under **reduced pressure, a series of tests was conducted in which the amount of silica added was varied from 4.3 wt % to** 14.7 wt & SiO<sub>2</sub>. The relative amounts of PbO and SiO<sub>2</sub> **contained in the slags correspond to the points labeled A, B, C, D, and E in Figure 29. In all of the tests made,** the concentration of Sb<sub>2</sub>0<sub>3</sub> was held constant at approxi**mately 30 wt % initially.**



**Figure 29. Phase Diagram for the PbO-rich End of the PbO~SiO2 System**

**The results from this series of tests are'presented in tabular form in Table 7 and shown in graphical form in Figures 30-34. Each test was repeated at temperatures of 750° and 850°C under a reduced pressure of 200y Hg. In tests RR and SS the molar ratio of PbO to EiO^ was adjusted to a value of 4, corresponding to the point A in Figure 29. It is apparent from Figure 30 that the rate of removal of** Sb<sub>2</sub>0<sub>3</sub> was approximately the same as that observed for the **most successful test made without silica additions for** test RR made at 750°C. Eighty gms of condensate were produced in this test which contained 98.71 wt % Sb<sub>2</sub>0<sub>3</sub> **(determined from PbO analysis). By increasing the tempera**ture to 850<sup>o</sup>C, an increased degree of removal of Sb<sub>2</sub>0<sub>3</sub> was obtained. Test SS resulted in a decrease in the Sb<sub>2</sub>0<sub>3</sub> con**tent of the slag from 33.7 wt % initially to 16.0 wt % at the end of the 8-hr period. This test produced 119 gms of** condensate which contained 93.86 wt % Sb<sub>2</sub>0<sub>3</sub>. The decreased **purity of the condensate was due to the increased volatilization of PbO at the higher temperature.**

The second pair of tests (VV and WW shown in Figure 31) was made with a molar ratio of Pb0 to SiO<sub>2</sub> of 2.91, corresponding to the eutectic composition between  $\beta$ -4Pb0'SiO<sub>2</sub> and 2PbO $\cdot$ SiO<sub>2</sub> shown as point B in Figure 29. A further increase in the degree of removal of  $\text{Sb}_2^0$  from the slag **was observed. The results of test VV, made at 750°C, are**

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**Figure 30. Removal of Sb from a 4,3 wt % SiO^~3O wt % Sb20 3-Pb0 Slag by Vacuum Distillation at 750° and 850°C**

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**Figure 31. Removal of Sb from a 5.6 wt % SiO^~3O wt % ^ 2^ 3~ph0 Slag by Vacuum Distillation at 750° and 850°C**

**somewhat erratic and are probably not representative. The** increased efficiency of removal is well-pronounced, how**ever, at 850°C in the results for test WW. The recovery of 8b^O^ in the condensate was slightly greater in these tests** than what was observed for tests RR and SS. The purity of **the condensates produced in these tests was also noticeably higher than was observed in tests RR and SS.**

The third and fourth pairs of tests (PP and QQ shown **in Figure 32 and XX and YY shown in Figure 33) were conducted on slags with a molar ratio of PbO to SiO^ of 2 and 1.47, respectively. A further increase in the degree of removal** of Sb<sub>2</sub>0<sub>3</sub> was observed for these tests over that obtained for tests VV and WW. The results of these 2 pairs of tests are **seen to be nearly identical at the respective temperatures and will be discussed together. The condensates produced in tests PP and XX contained approximately 70% of the original** amount of Sb<sub>2</sub>0<sub>3</sub> contained in the slag at a purity of 99 wt % **2b^O^ or higher. The condensates produced in tests QQ and Y Y , made at 850°C accounted for a recovery of approximately** 87% of the  $\text{Sb}_2\text{O}_3$  at a purity of greater than 98 wt %  $\text{Sb}_2\text{O}_3$ .

Because of the high degree of removal of  $\text{Sb}_2\text{O}_3$  from **slags containing 8.2 and 10.5 wt % BiO^, tests PP and** *QQ* **were duplicated at greatly reduced pressure under the same conditions of temperature. The results of these tests (AD and AC) , made at a pressure of 5p IIg , have been included**



**t, hr**

Figure 32. Removal of Sb from a 8.2 wt % SiO<sub>2</sub>-30 wt % **Sb20 3~PbO Slag by Vacuum Distillation at 750° and 850°C**



Figure 33. Removal of Sb from a 10.5 wt % Si0<sub>2</sub>-30 wt % **S^)2^3"P^^ S lag by Vacuum Distillation at 750° and 850°C**

**in Figure 32 for comparison with tests PP and QQ. It is readily apparent that the decreased pressure results in a** much more efficient removal of  $Sb_20_3$ . Because of this very **low pressure, however, the increased volatilization of PbO results in a significantly reduced purity of the condensate. In both tests AB and AC the concentration of PbO in the condensate was approximately 5 wt %.**

**In order to complete the investigation of the effects** of silica additions on the rate of removal of  $Sb_2^0$  from **lead-softening slags under reduced pressure at elevated temperatures, a final pair of tests was conducted in which** the molar ratio of Pb0 to Si0<sub>2</sub> was held at a value of 1. **This ratio corresponds to the point E on the phase diagram for the Pb0-Si02 system shown in Figure 29. The greatly increased viscosity of this melt resulted in a much less** efficient removal of Sb<sub>2</sub>0<sub>3</sub> as shown by the results for **tests TT and UU presented in Figure 34. The purity of the condensates produced in these 2 tests was the highest, however, for the condensates produced in this series of tests. Test TT yielded 73 gms of condensate containing 99.5 wt %** Sb<sub>2</sub>0<sub>3</sub> while test UU yielded 107 gms of condensate contain**ing 99.25 wt % 2»**

**Quantitative information regarding the intermolecular forces in complex Pb-silicate melts would be helpful in** explaining the relative ease with which  $Sb_2^0$  could be

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**Figure 34. Removal of Sb from a 14.7 wt % SiO^~3O wt %** Sb<sub>2</sub><sup>0</sup><sub>3</sub>-Pb0 Slag by Vacuum Distillation at **750° and 850° C**

distilled from Pb0-Si0<sub>2</sub>-Sb<sub>2</sub>0<sub>3</sub> slags. However, due to a **general lack of such information in the literature, no such discussion can be made here. It is possible, however, to make the qualitative statement that as the concentration of Si02 in these ternary slags is increased from 4.3 wt % to 10.5 wt %, the degree to which ôb^O^ can be distilled from them under reduced pressure is correspondingly increased.** As the concentration of  $\text{SiO}_2$  is increased above 10.5 wt %, the vacuum removal of  $Sb_2^0$  becomes less efficient.

In order to compare the rates at which  $Sb_2^0$  can be **distilled from lead softening slags which contain silica additions and those which do not, some quantitative infor**mation regarding the vapor pressure of  $Sb^0_40^0_6$  above these **slags is required. It was for this purpose that the PbO to** SiO<sub>2</sub> ratio of 2 was selected for the vapor pressure study of Pb0-Si0<sub>2</sub>-Sb<sub>2</sub>0<sub>3</sub> slags discussed in a previous section. **In referring to Figure 23, it is seen that the vapor pres**sure of  $\text{Sb}_{4}$ <sup>0</sup> $\text{G}_{6}$  above the Pb-silicate slags at 700<sup>o</sup>C is greater than that above the binary  $Sb_2^03^{-Pb0}$  slags at all compositions above approximately  $X_{Sb_2 0_3} = 0.21$  (on Pb0 + Sb<sub>2</sub>0<sub>3</sub> basis). This difference in vapor pressure accounts for the more rapid initial rate of removal of  $Sb_2^0$ <sub>3</sub> observed **in the case of the slags containing silica over those which do not. Using Equation (16) and the equilibrium SD2O 3 '2** content for a Pb0-Si0<sub>2</sub>-Sb<sub>2</sub>0<sub>3</sub> ( $\frac{1}{S100}$  = 2) slag in contact

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with Pb at 700<sup>O</sup>C (test BF, Table 8),  $a_{Pb0}$  is calculated to be 0.571 (on Pb0+Sb<sub>2</sub>0<sub>3</sub> basis). A similar calculation has been made for the Pb0-Sb<sub>2</sub>0<sub>3</sub> system for  $X_{Sb203} = 0.0683$  with the result that  $a_{Pb0} = 0.964$ . Thus, it is apparent that the addition of  $SiO_2$  to  $Pb0-Sb_2O_3$  slags results in an **increase in the purity of the condensate due to the resulting decrease in the activity, and hence vapor pressure, of PbO.**

The fact that the concentration of Sb<sub>2</sub>0<sub>3</sub> can be reduced **to much lower levels when silica is present is almost entirely due to the greatly increased fluidity of the silica-based slags. The very viscous nature of the binary** Pb0-Sb<sub>2</sub>0<sub>3</sub> slags prevented the stirring action from constantly replenishing the surface of the melt with  $\text{Sb}_2\text{O}_3$ . As a result, the transport of  $Sb_0^0$  from the bulk solution **to the surface of the melt became the rate determining step which controlled the actual rate of removal. Because of the very fluid nature of the majority of the Pbsilicate slags, stirring was very effective and the con**centration of  $\text{Sb}_{2}$ <sup>0</sup>  $\text{S}$  was observed to be decreased to much **lower levels than was observed for the slags containing no silica additions,**

**Accurate mass balances on the tests described above,** from which the  $\frac{1}{8}$  recovery of  $Sb^0$ <sub>2</sub> could be calculated, **could not be made in this investigation. The recoveries** **mentioned above are meant to be only approximate values. Due to the formation of iron oxides on the crucibles used for the tests during cleaning, a significant amount of Pb metal was formed in some of the tests. The amount of Pb formed by reduction of PbO by FeO varied with the condition of the crucible and the temperature at which the tests were carried out. No reduction of PbO was observed with new crucibles. As much as 30 gms of Pb were produced in some of the tests made at 350°C. Also, some of the Pb and PbO present in the crucible vaporized and was observed to condense in the hotter, lower portion of the condenser where the PbO reacted with the silica and thus could not be recovered for weighing.**

**Based on the results of the tests described in the previous section, a process using reduced pressure at elevated** temperature has been developed in which the  $Sb_20_3$  content of a 30 wt % Sb<sub>2</sub>0<sub>3</sub>-Pb0 slag can be reduced to 10 wt % or **slightly less in a period of 8 hrs at 200p Hg pressure.** The Sb<sub>2</sub>0<sub>3</sub> can be recovered as a dense, non-adhering condensate containing in excess of 99 wt % Sb<sub>2</sub>0<sub>3</sub>.

**The conditions under which this process works best are as follows :**

- **1) temperature 750oC**
- **2) pressure 200y Hg**
- 3) slag addition agents  $8-10$  wt  $8$  SiO<sub>2</sub>

**4) residual atmosphere - inert**

The degree of removal of Sb<sub>2</sub>0<sub>3</sub> will be increased as **either the temperature is increased or the pressure is decreased. The purity of the condensate produced will decrease in either case, however.**

## Selected Slag-Metal Equilibria in the Sb<sub>2</sub>0<sub>3</sub>-SiO<sub>2</sub>-PbO System

**The process described in the preceding section for the** recovery of Sb<sub>2</sub>0<sub>3</sub> from lead-softening slags has the disadvantage of leaving a somewhat high Sb<sub>2</sub>0<sub>3</sub> content in the **residual slag. As a result, it might be desirable to recover both the Sb and Pb values remaining. An ideal way of achieving this result would be to use the residual slag for softening additional Pb bullion. After this operation, the slag could be returned for further vacuum treatment for** the recovery of the  $\text{Sb}_2\text{O}_3$ . A cyclic process such as this **would have the advantage of being able to use a small recirculating slag volume which would greatly reduce the slag and dross handling problems normally encountered with the softening of Pb bullion.**

**The results of several slag-metal equilibrations carried out for PbO-EiO^-Eb^O^ slags in contact with dilute Pb-Sb alloys are given in tabular form in Table 8. The results of these tests indicate that the Pb-silicate slags** produced in the vacuum removal of Sb<sub>2</sub>0<sub>3</sub> tests are not

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**capable of softening Pb bullion to any considerable extent. The equilibrium Sb contents are all much too high to yield a refined Pb metal of acceptable purity.**

**A second alternative to the disposal of these slags would be to add them directly to the lead blast furnace using Fe as a reducing agent. If a sufficient market for antimonia1-Pb exists, these slags may also be converted to this product in a separate reverberatory smelting operation in which the Pb-silicate slags would be reduced by Fe and carbon.**

Vapor Pressure of As<sub>A</sub> above Dilute As-Pb Alloys at  $703^{\circ}$ C

**The removal of As from lead-softening slags as the trivaient oxide by the application of vacuum techniques was shown not to be feasible by the results of tests described in an earlier section. Since the vapor pressure of As^ above pure As is known to be very high, the application of vacuum techniques to the removal of elemental As from Pb bullion might provide an alternative method by which lead could be softened, at least insofar as As is concerned.**

**The literature contains almost no information regarding attempts by earlier workers to remove As from Pb by vacuum distillation. Caldwell, Spendlove, and St. Claire (19 60, pp. 1- 12) have studied the vacuum distillation of Cd, Zn, Mg, Te, Sb, and As from Pb and Sn over a range of**

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**temperatures. No mention is made, however, as to whether As was successfully removed from the alloys supposedly studied. They have determined that Sb could not be removed from a 2.3 wt % Sb-Pb alloy at 1000°C.**

**In view of the lack of experimental data regarding the vaporization of As from Pb-As alloys, a somewhat limited vapor pressure study was made on alloys containing from 0.5 wt % to 3.3 wt % As in Pb. The results of this study are given in tabular form in Table 5 and shown graphically in Figure 10. The vapor phase above pure As at 703°C is** composed of a mixture of As<sub>4</sub>, As<sub>2</sub>, and As. The vapor pressures of As<sub>2</sub> and As are, however, negligible with respect to the pressure of As<sub>4</sub>. The sublimation temperature of As **is given by Elliott and Gleiser (1960, p. 19) as 6 13°C and the melting point as 817°C under a pressure of approximately 2 8 atm.**

**The results given in Table 5 have been replotted in Figure 35 together with values of**  $X \cdot p_{As_A}^O$  **(for an ideal As<sub>4</sub>** solution) for comparison. The vapor pressure of As<sub>4</sub> **above pure As at 703°C (referred to the hypothetical, supercooled liquid) is calculated to be 16,720 mm Hg using the data of Elliott and Gleiser for the heats of sublimation and fusion of As, It is readily apparent from Figure 35** that the vapor pressure of  $As_A$  above dilute Pb-As alloys is **much too low for the efficient removal of As from such**



Vapor Pressure of As<sub>4</sub> above Dilute Pb-As Alloys at  $703^{\circ}$ C Figure 35.

**alloys to concentrations much below 1 wt % As. Since the concentration of As in Pb blast-furnace bullion rarely exceeds 1 wt %, the application of vacuum techniques to the removal of As from Pb does not appear to warrant further investigation.**

**The data presented in Table 5 can be converted into the** . thermodynamic activity of As in Pb by division of  $p_{As_A}$  by **p0 = 16,720 mm Hg and taking the fourth root of the As 4 resulting pressure ratio. A Gibbs-Duhem integration of these activity data is presented in Table 17. A plot of the a-function for As in Pb is shown in Figure 36. It can be seen from the data of Table 17 and Figure 36 that the** behaviour of As in dilute Pb-As alloys at 703<sup>°</sup>C is charac**terized by a near approach to ideality. Furthermore, it would appear that a regular solution model for the Pb-As system at 703°C would be a good approximation for the system for compositions above 5 mole % As due to the near-constant value of the a-function with composition. Although the slope of the a-function with composition appears to be zero for a portion of the composition range studied in this investigation, it is not safe to assume a regular solution model due to the rather narrow limits of the As concentration range. The apparent outlier represented by the alloy containing 1.43 mole % As is a result of** the fact that the vapor pressure of As<sub>4</sub> above the alloy **was barely detectable by the experimental**





\* Completion of this procedure to obtain a<sub>pb</sub> is of no value due to the small<br>number of closely-spaced data points.



**Figure 36. Variation of the As a-function with Composition for the Pb-As System at 703°C**

**procedure used in this investigation. Because of this, the apparent vapor pressure determined for this alloy could be in considerable error.**

**The activity of As in Pb determined in this investigation cannot be directly compared with the results of any previous investigators. As was mentioned previously, the literature contains very little information concerning the activity of As in Pb. J. H. Richards, Imperial Smelting Corporation Ltd. (196 8, private communication) has described some thermodynamic investigations of dilute Pb-As alloys in the temperature range from 900°-1100°C. His results** indicate similar pressure-composition relationships to those **reported in this investigation. Moriyama and coworkers (196 4, pp. 191-4) have also investigated the Pb-As system at temperatures from 450o-600°C. As a result of an emf study, they have found that the activity of Pb in this system shows a positive deviation from ideality over the entire composition range studied. The behavior of As was found to be characterized by a strong positive deviation from ideality. Since a detailed account of their work is not readily available, no English translation having been made of the original Japanese article, a thorough investigation of their results is not possible.**

**The activity of As in Pb determined in this investigation can be successfully predicted from the phase diagram**

**for the Pb-As system» The phase diagram consists of a single eutectic located at 7.6 wt % As at a temperature of** 289<sup>°</sup>C. No compounds are known to exist between Pb and As, **and no solid solubility has been reported for either As in Pb or Pb in As. Calculations for** *y°* **, using the Clausius-As Clapeyron equation for freezing-point depression, have . been made in the past by a number of investigators, among** them Davey (1963, pp. 514-5). The results of such a calcu**lation are shown in Figure 37. It is readily apparent from the figure that the regular-solution model used for the calculation represents a good approximation for a value** of  $\gamma^{\circ}_{\text{As}}$  comparable to the values for the activity coefficient **of As in dilute Pb-As alloys as determined in this investigation. Although the data of this investigation are some**what limited, they indicate that  $\gamma_{AS}^{O}$  might be slightly **greater than unity. This would agree with the results of Moriyama and coworkers obtained at lower temperatures.**

**The results shown in Figure 38 represent an attempt to** determine  $\gamma_{\text{AS}}^{\text{O}}$  in the Pb-As system at 703<sup>o</sup>C. The very steep **curvature observed at very low arsenic concentrations does not allow an accurate extrapolation to zero As concentration, however.**

**The results of this investigation, although far from complete, show that As in dilute Pb-As alloys at 703°C exhibits near-ideal-solution behavior. Because the vapor**

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 $X_{\text{As}}$ 

**Figure 37. Activity of As in the Pb-As System at 703°C (Standard state - pure, hypothetical, supercooled liquid As)**



Figure 38. Variation of  $ln\gamma$ <sub>As</sub> with Composition for the **Pb-As System at 703°C**

pressure of As<sub>4</sub> above Pb-As alloys is equal to  $p_{As_4}^{\circ}$  ( $a_{As}$ )<sup>4</sup>, **ideality with respect to As does not insure a high pressure** of As<sub>4</sub> above the alloys. As a result, the vacuum distil**lation of As from Pb biast~furnace bullion containing small amounts of dissolved As would not appear to be technically " feasible at a temperature near 700°C.**

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## **CONCLUSIONS**

**On the basis of the experimental results obtained in this investigation, several conclusions can be made and several bases for further investigation can be proposed.**

**The vapor-pressure determinations which have been made** in this investigation for the PbO-Sb<sub>2</sub>O<sub>3</sub> system show that the behavior of Sb<sub>2</sub><sup>0</sup><sub>3</sub> is characterized by a strong negative **deviation from ideality at all compositions below 50 mole % ^b^O^ at 700°C. The behavior of PbO is characterized by a positive deviation from ideality at all compositions above approximately 63 mole % PbO and by a negative deviation from ideality in the range from 63 mole % to 50 mole %** Pb0 at  $700^{\circ}$ C. In the Pb0-Si0<sub>2</sub>-Sb<sub>2</sub>0<sub>3</sub> ( $\frac{Pb0}{Sio_2}$  = 2) system, Sb<sub>2</sub>0<sub>3</sub> **exhibits a negative deviation from ideality at all com**positions below 25 mole % Sb<sub>2</sub>0<sub>3</sub>. The slag systems do not **form an ideal or a regular solution in either case•**

Since the activities of both PbO and SiO<sub>2</sub> have been **determined in the PbO-SiO^ system by other investigators,** the activity study in the  $Pb0-Sb^{0}_{2}$  system reported in this **investigation should be extended through the remainder of the system before suitable data can be obtained to yield**

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**the individual component activities in the ternary**  $Pb0-Si0<sub>2</sub>-Sb<sub>2</sub>0<sub>3</sub>$  system.

**In the temperature range from 650° to 750°C, the** standard free energy of formation of liquid  $Sb_20_3$  is given by the expression:  $\Delta G^{\circ}$  = -159,190 + 56.20 T. The **equilibrium constant for the reaction:**

 $2 \frac{\text{Sb}}{\text{L}}(1 \text{ wt } 8 \text{ in Pb}) + 3 \text{ Pb}(1) = \text{Sb}_2 0_{3(1)} + 3 \text{ Pb}(1)$ is given by the expression: log  $K_{eq} = \frac{4980}{T} - 4.165$ , for **the temperature range from 650° to 750°C. The standard** free energy of formation of  $Pb0 \cdot Sb^{0}$  from the elements at **604°C is calculated to be -146,580 cal.**

**The vacuum-removal experiments conducted in this investigation show that As and Sn cannot be efficiently removed as oxides from artificial lead-softening slags by vacuum distillation at the concentrations and temperatures normally encountered in the conventional fire-refining of lead.**

**A set of optimum conditions was determined to treat an** artificial lead-softening slag containing 30 wt % Sb<sub>2</sub>0<sub>3</sub>. **These optimum conditions were 200p Hg pressure, or lower,** and an addition of SiO<sub>2</sub> of from 8-11 wt % SiO<sub>2</sub>. The process **was successful in removing approximately 80 wt % of the original Gb^O^ content of the slag in 8 hr and producing a** condensate containing in excess of 98 wt  $8 \text{ Sb}_2^0$  at **temperatures of 750° and 850°C.**

**Several tests conducted in this investigation showed that successful recovery of Sb as the volatile trioxide from artificial lead-softening slags might be achieved at temperatures below the melting point of the slags. A full-scale investigation of this method would be necessary % to determine if it would present major advantages over the process outlined above.**

**The vapor-pressure determinations made in this investigation for the Pb-As system show that As exhibits nearideal- solution behavior, in agreement with the phase diagram at 700°C. In view of the experimental results obtained, the vacuum distillation of As from very dilute Pb-As alloys at 700°C does not appear to be technically feasible in spite of the very high vapor pressure of pure As at this temperature.**

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## **SUMMARY**

The vapor pressure of Sb<sub>4</sub>0<sub>6</sub> was determined above Pb0- $Sb_00$ , and Pb0-Si0<sub>2</sub>-Sb<sub>2</sub>0, ( $\frac{FDO}{P}$  = 2) slags at 700°C. The *^ 3 z* **^ J Sio2 thermodynamic activity of Sb^O^ in both slag systems was calculated using the measured vapor-pressure data. In the** Pb0-Sb<sub>2</sub>0<sub>3</sub> slag system, Sb<sub>2</sub>0<sub>3</sub> was found to show a negative **deviation from ideality at all slag compositions below 50** mole %  $Sb_20$ <sub>3</sub>. The behavior of PbO was found to be mixed. Activity coefficients for Pb0, calculated by means of a Gibbs-Duhem integration of the Sb<sub>2</sub>0<sub>3</sub> activity data, were **found to exceed unity at all slag compositions above approximately 63 mole % PbO. At slag compositions between 63 mole % and 50 mole % PbO, activity coefficients were** found to be less than unity. In the  $Pb0-Si0^2-Sb^20^3$  $(\frac{200}{\sqrt{3}})$  = 2) slag system,  $\text{Sb}_0\text{O}_3$  was found to show a negative Sio<sub>2</sub>  $\cdot$  <sup>3</sup> <sup>3</sup> <sup>3</sup> 4 3 **deviation from ideality at all slag compositions below** 25 mole  $\delta$  Sb<sub>2</sub><sup>0</sup><sub>3</sub>. A calculation for the activities of Pb0 **and SiÛ2 in the silicate slag system was not possible due to a lack of sufficient data.**

The vapor pressure of  $Sb_4^0$ <sub>6</sub> above pure, solid, cubic  $Sb<sub>2</sub>0<sub>3</sub>$  was determined for the temperature range from  $422^{\circ}$  to

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**599°C. The logarithm of the measured vapor pressure above cubic ^b^O^ v/as observed to vary directly with reciprocal absolute temperature.**

Tests were made on the rate of removal of As, Sb, and Sn **as oxides from 500 gm of 3 wt % 3 wt %** *As***203"** 30 wt %  $\text{Sb}_2\text{0}_3-\text{Pb0}$ , 30 wt %  $\text{Sb}_2\text{0}_3-\text{Pb0}$ , and 3 wt %  $\text{As}_2\text{0}_3$ **30 wt % Sb203-10 wt % Sn02~Pb0 artificial lead-softening slags under reduced pressure conditions at temperatures between 500° and 350°C. The results of these tests indicated that successful removal of As and Sn as oxides, at the concentrations studied in this investigation, was not tech**nically feasible at a reduced pressure of 200µ Hg. The results obtained for Sb, however, suggested the possibility **of removing Sb as the volatile trioxide under a reduced pressure of** *200\i* **Hg at temperatures above 700°C.**

**As a means of increasing the recovery of Sb from PbObase slags, tests were made on the rate of removal of Sb** from slags containing a variable Si0<sub>2</sub> content. The addition of SiO<sub>2</sub> to lead-softening slags improves the recovery of Sb as the volatile trioxide by increasing the activity of Sb<sub>2</sub>0<sub>3</sub> in the slag at compositions greater than 13 mole % Sb<sub>2</sub>0<sub>3</sub>. **In addition, it was observed that the increased fluidity of** the slags containing an optimum SiO<sub>2</sub> concentration accounted for an increased rate of removal of Sb at low Sb<sub>2</sub>0<sub>3</sub> concentrations where the activity of  $Sb<sub>2</sub>0<sub>3</sub>$  was lewer than that

**determined for the slags containing no SiO^ additions. The purity of the condensates produced during the tests made on** slags containing SiO<sub>2</sub> additions was also found to be higher than that observed for similar slags containing no SiO<sub>2</sub> due **to a reduction in the activity of PbO, and hence its vapor pressure.**

**A set of optimum conditions was determined to treat an** artificial lead-softening slag containing 30 wt % Sb<sub>2</sub>0<sub>3</sub>. **These optimura conditions were 200p Hg pressure and an addi**tion of  $\text{SiO}_2$  of from 8-11 wt %  $\text{SiO}_2$ . The process was **successful in removing approximately 80 wt** *%* **of the original ^1>2^3 content of the slag in 8 hr and producing a condensate** containing in excess of 98 wt % Sb<sub>2</sub>0<sub>3</sub> at temperatures of **750° and 850°C.**

Finally, the vapor pressure of As<sub>A</sub> was determined above **dilute Pb-As alloys at 703°C as a preliminary study to a full-scale investigation of the vaporization of As from Pb-As alloys. The study proved the impossibility of recovering As from Pb-As alloys containing less than about 3 mole % As by vacuum distillation under moderately reduced pressures at 703°C. The experimental results, when converted to As activities, show that the behavior of As in Pb-As alloys containing less than 10 mole % As is characterized by near-ideal-solution behavior at 703°C.**

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## **APPENDICES**







**Appendix II. Methods of Chemical Analysis**

- **A. Chemical Analysis for As and Sb in Lead Oxide Slags hy the Distillation-Bromate Method (ASTM Analysis E 46-66) ;**
	- **1. A 0.25 gm sample was transferred to a 500 ml Erlenraeyer flask.**
	- **2. To the flask and to a second flask carried, through the procedure as a blank, 15 gm KIISO^** and 20  $\text{ml H}_2\text{SO}_4$  were added.
	- **3. The flask was gently heated to decompose the sample, and when decomposition was complete, it was strongly heated over an open flame to expel or wash down the sulfur on the walls of the flask.**
	- **4. The flask was then cooled and 10 ml 1^0 were** added to hydrate the H<sub>2</sub>SO<sub>4</sub>. The sample was **finally cooled to room temperature.**
	- **5. 50 ml IIC1 and 10 gm NaCl were added to the flask.**
	- **6 . The flask was connected to the distillation apparatus (see figure below) and 200 ml 1^0 were added to the receiving beaker. The distillation flask was heated on a hot plate until the temperature of the vapor inside the flask reached 105°C. The distillation flask was then disconnected and removed from the hot plate.**

 $\cdot$ 



- **7• The distillate was heated to boiling and boiled gently for 10 rain to expel sulfur compounds,**
- **8 , The distillate was then titrated at 80-90°C** with 0.1N KBrO<sub>3</sub> solution and methyl orange indicator added near the end of the titration.
- **9.** This titration determined As<sub>2</sub>0<sub>3</sub> in Pb0-slags **by the following formula:**

wt % As<sub>2</sub>0<sub>3</sub> = 
$$
\frac{(\Lambda - B)(0.1) (0.0375) (100)}{C} \times 1.32
$$

\nwhere: A = m1 KBr0<sub>3</sub> to titrate sample

\nB = m1 KBr0<sub>3</sub> to titrate blank

\nC = wt of sample in gm

- **1 0 . To the solution remaining in the distillation flask, 25 gm NaCl were added and the solution diluted to 350 ml with boiling water,**
- **11. The solution was titrated hot with 0.1N KBrO3 and methyl orange indicator.**

- 12. This titration determined Sb<sub>2</sub>0<sub>3</sub> in Pb0-slags by **the following formula:** wt %  $\text{Sb}_2\text{O}_3 = \frac{(\text{A-B}) (0.1) (0.0609) (100)}{\text{C}} \times 1.20$ where:  $A = mL KBr0^3$  to titrate sample  $B = mL KBr0<sub>3</sub>$  to titrate blank **C = wt of sample in gm**
- **B. Chemical Analysis for As and Sb in Pb by the Distillation-B rornate Method: The same method as outlined above was used to determine As and Sb in Pb with the exceptions that 1,0 gm** samples and 0.01M KBrO<sub>3</sub> were used. The calculations **for wt % As and wt % Sb were modified as follows :**  $W t$  % As =  $\frac{(A - B) (0.01) (0.0375) (100)}{x}$  x 1.3  $\overline{c}$ **and,**  $\sqrt{2}$   $\sqrt{2$

$$
\text{wt 8 Sb} = \frac{(\text{A-B}) (0.01) (0.0609) (100)}{\text{C}} \times 1.20
$$

- **C. Chemical Analysis for Sn by the lodimetric Titration Method (ASTM Analysis E57-60):**
	- **1. A 1,0 gm sample was transferred to a 500 ml Erlenraeyer flask.**
	- **2. To the flask and to a second flask carried** through the procedure as a blank, 5 gm KHSO<sub>4</sub> and **20 ml H 2SO 4 were added,**
	- **3. The flask was gently heated to decompose the sample, and when decomposition was complete, it**

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**was strongly heated over an open flame to expel or wash down the sulfur on the walls of the flask.**

- **4. The flask was then cooled and 180 ml II20 were added.**
- **5. 60 ml IIC1 and 10 gm pure Fe wire were added to the flask.**
- **6. The flask was connected to the distillation** apparatus (described above) and a saturated NaHCO<sub>3</sub> **solution was added to the receiving beaker. The contents of the flask were heated to boiling and boiled for 30 min (some undissolved Fe should remain after boiling).**
- **7. When reduction was complete, the contents of the** flask were cooled to  $10^{\circ}$  ±  $2^{\circ}$ C under a CO<sub>2</sub> at**mosphere.**
- **8.** Maintaining the CO<sub>2</sub> atmosphere, 5 ml starch solu**tion were added to the flask and the solution was titrated in the presence of Fe with standard**ized KI0<sub>3</sub> solution.

**This titration determined Sn02 in PbO-slags by the following formula:**

wt 
$$
\$
$$
 Sn0<sub>2</sub> =  $\frac{(A) (B) (100)}{C}$  x 1.27

- $\cdot$  where:  $A = mL KIO_3$  to titrate sample
	- $B = Sn$  equivalent of KI0<sub>3</sub> solution **(0.0594 gm/ml)**

**C = wt of sample in gm**

- 10. The standard KIO<sub>3</sub> solution was prepared as follows: 3.5670 gm KIO<sub>3</sub> were dissolved in **200.0 ml h^O containing 1.0 gm NaOII; 10.0 gm KI were then added to the solution. The resulting solution was added to a 1000 ml flask and diluted with water to 1000.0 ml. This solution was then standardized against** a known SnO<sub>2</sub>-PbO slag.
- **11. The starch solution was prepared as follows : 0 « 80 gm soluble starch was dissolved in 400 ml hot h^O and allowed to cool to room temperature. The starch solution was prepared fresh daily.**
- **D. Chemical Analysis for Pb and Sb in Oxide Condensates by Atomic Absorption Techniques :**
	- **1. A 0,5 gm sample v/as weighed** *Into* **a 150 ml beaker.**
	- 2. 10 ml of a mixture of conc. HCl and conc. HNO<sub>3</sub> **(10:1) was added to the samples and allowed to stand overnight with intermittent swirling at room temperature.**
	- **3. 20 ml of a 10% tartaric acid solution was added to the samples, with stirring, and the samples quantitatively transferred to 100 ml volumetric flasks and diluted to volume with distilled v/ater.**
	- 4. Suitable aliquotes were then taken for analysis.

- 5. Standard solutions were prepared from B & A **test lead metal (99.99+% Pb) and Sb métal (AS&R 99.999+% Sb). Solution was affected in the same manner as described above. The standard samples were diluted to the concentrations desired for calibration of the atomic absorption spectrophotometer.**
- **6. Conditions for obtaining the calibration curve for Sb were as follows : Instrument — Perkin-EImer Model 303 Atomic Absorption Spectrophotometer o Wavelength -- 2311.5 A Slit — 3-2 Source and Current — Australian-made hollow cathode lamp at 20 ma.** Fuel -- acetylene at 8 psi **Oxidant — air at 30 psi Burner — 3-slot Boling Burner head**
- **7. The data for the calibration curve for the Sb analyses is as follows :**

**log % absorption yi gm Sb/ml**



Appendix III. Sample Calculation for p<sub>Cd</sub> above pure Cd **from Weight-loss Data**

**The molecular weight of Cd is 112,40 gm/mol,**

$$
P_{\text{Cd}} \text{ (atm)} = \frac{n_{\text{Cd}}}{n_{\text{argon}}} P_{\text{t}} \text{ (atm)}
$$
 (if  $n_{\text{Cd}} < n_{\text{argon}}$ )  

$$
n_{\text{Cd}} = \frac{\Delta w_{\text{r}} \text{ gm}}{112,40}
$$

**Assuming that argon behaves as an ideal gas,**

$$
n_{\text{argon}} = \frac{P_{t}V}{RT_{r}}
$$
\n
$$
\text{Therefore, } P_{Cd} \text{ (mm Hg)} = \frac{(\Delta w, gm) (P_{t}, atm) (760) RT_{r}}{(P_{t}, atm) (V, litres) (112.40)}
$$
\n
$$
P_{Cd} \text{ (mm Hg)} = \frac{(\Delta w, mg) (0.03205) (760) T_{r}}{(V, litres) (112.40) (1000 mg/gm)}
$$
\n
$$
P_{Cd} \text{ (mm Hg)} = \frac{(\Delta w, mg)}{(V, litres)} \times T_{r} \times 5.550 \times 10^{-4}
$$

where:  $T_r$  = temperature at which volume of argon was **measured, °K.**









1. Cadmium Cont'd



 $\frac{1}{2}$ 



 $2.8b_20_3$ 





 $\ddot{\phantom{0}}$ ť  $\epsilon$ ó

 $\ddot{\phantom{0}}$ 



 $\ddot{\phantom{a}}$ 



 $\mathrm{Sb}_2$ <sup>0</sup>3 Cont'd.  $\frac{1}{2}$ 





 $\bullet$ 

 $2.$   $Sb<sub>2</sub>0<sub>3</sub>$  Cont'd.





 $3.$  Pb0-Sb<sub>2</sub>0<sub>3</sub> slags



 $\hat{\mathcal{F}}$


3. Ph0-Sh<sub>2</sub>0<sub>3</sub> slags Cont'd.





 $\ddot{\phantom{0}}$ 

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Appendix IV. Cont'd.

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Cont'd.  $4.20 - 510 - 5522$ 



 $\bar{\mathcal{A}}$ 



slags Cont'd.  $Pb0-Si0-5b-0 \ddot{q}$ 



 $\mathcal{F}_{\mathcal{G}}$ 



5. Pb-As alloys

Test	$\mathbf{x}_{\texttt{As}}$	Temp, $\circ$	Room Temp,	Flow Rate, cc/min	<b>STP</b> Rate $\frac{1}{2}$ F1ow cc/min	Reaction Time, min	grans	mg/liter ٠ Weight loss
C $\lambda$	0.0690	703	27	99	74	$\frac{1}{2}$	ო ທ .111 $\circ$	882* $\bullet$ ო
$A - 4$	0.0690	703	$\frac{8}{2}$	120.5	O Q	m $\bullet$ 25	$\circ$ 0.0113	667* $\bullet$ $\mathsf{m}$
m $\mathbf{k}$	0.0690	703	29	141	105	23	ო نب $-0.12$ . $\circ$	$\frac{*}{3}$ $\omega$ $\infty$ ٠ ო
$A - 6$	0.0690	703	$\frac{5}{2}$	84	63	ನ	c ທ Ō $0.00 - 0.0$	$\frac{*}{0}$ $\infty$ $\circ$ • ෆ
$A - 7$	0690 $\mathbf{c}$	703	29	67	50	32	$\mathbf{r}$ $\blacksquare$ $\sigma$ 00. $\circ$	c 4 $\mathbf{\Omega}$ ٠ 4
$\infty$ $\lambda$	0.0690	703	29	ო $\overline{\mathbf{r}}$	32	ನ	609 $\overline{O}$ $\bullet$ O	$\frac{6}{3}$ ທ ٠ 4
$A-9$	0.0690	703	24	178	133	$\vec{c}$	0.01322	$\circ$ .39 $\overline{\mathcal{C}}$
급 $A -$	0.0279	703	29	5 $\overline{\mathbf{v}}$	ທ $\frac{1}{2}$	48	ᆏ 4 0.000	$\mathbf{\Omega}$ $\ddot{\phantom{0}}$ $\dot{\mathbf{c}}$ $\ddot{\circ}$
12 $\mathbf{A}$	0.0279	703	29	ທ $\bullet$ $\Omega$ Ą,	34	50	0.00055	× 42 $\overline{\mathbf{c}}$ $\mathbf{c}$
14 $\mathbf{A}$	0279 $\mathbf{c}$	703	29	ഗ Ó $\overline{\mathbf{c}}$	Ŋ $\sim$	$^{\circ}$ $\overline{5}$	45 000 $\bullet$ $\circ$	$\ddot{\phantom{1}}$ $\sim$ ო $\sim$ $\bullet$ $\bullet$
$\mathbf{r}$ $\frac{1}{\mathcal{A}}$	0.0279	703	$\frac{8}{2}$	77	ທ 57.	97	$\overline{6}$ 0.0000	$\ast$ $\circ$ 4 $\mathbf{\Omega}$ $\bullet$ $\circ$
$A - 16$	0.0279	703	28	105	n 78.	50	136 0.00	$\rm{^*}$ 22( $\bullet$ Ó
$A-17$	0.0279	703	29	135	101	55	0.00130	.175 $\circ$

 $\ddot{\phantom{0}}$ 



5. Pb-As alloys Cont'd.





Cont'd. Pb-As alloys  $\mathbf{5}$ 







Appendix V. X-ray Powder Diffraction Data for Pb0, Pb, Sb,  $\text{Sb}_2$ 0<sub>3</sub>,  $\text{Sb}_2$ 0<sub>4</sub>,  $\text{Sb}_2$ 0<sub>5</sub>, As, As<sub>2</sub>0<sub>3</sub>, As<sub>2</sub>0<sub>5</sub>, Sn, Sn0<sub>2</sub>,  $2Pb0 \cdot Si0_2$ ,  $\alpha - 4Pb0 \cdot Si0_2$ , and  $\gamma - 4Pb0 \cdot Si0_2$  as **Compiled from the ASTM Powder Data Index**



$d_{hk1}$	$2\theta$ ,	Relative Intensity
$\text{A}^\text{O}$		
5.90 4.46	15.00 19.88	3 9
3.445 3,073	25.84 29.04	3 35 100
2.942 2.718	30.36 32.92	5 45 9
2.470 2.404 2.235	36.34 37.38 40.32	25 $\overline{\mathcal{U}}$ 17 11
5.952 3.108 2.976 2.577 2.365 2.102	14.86 28.70 30.00 34.78 38.02 43.00	25 20 100 30 4 $\overline{\mathbf{c}}$
3.52 3.112 2.771 2.050	25.28 28.66 32.28 44.14	26 6 100 24
6.394 3.920 3.195 2,768 2.541 2,262 2.132	13.84 22.66 27.90 32.32 35.28 39.82 42.36	63 $\leq$ 1 100 28 38 12 17
7.1 5.6 4.88 4.01 3.58 3.40 3.21 3.05 2.70 2.62	12.46 15.80 18.16 22.16 24,84 26.18 27.76 29.26 33.14 34.20	30 30 100 10 60 60 20 50 20 40 10
	3.60 3.033 2.651 2.34	$\circ$ 24.70 29.42 33.78 38.42

**Appendix V Cont1d.**

Element	$d_{hk1}$	$2\theta$ , $\circ$	Relative Intensity
or Compound	$A^O$		
$\alpha$ -Sn	3.751	23.70	100
	2.294	39.24	83
	1.956	46.38	53
$\beta - Sn$	2.915	30.64	100
	2.793	32.02	90
	2.062	43.87	34
Sn0 <sub>2</sub>	3.351	26.58	100
	2.644	33.88	81
	2.369	37.95	24
	2.309	38.98	5
	2.120	42.61	$\overline{2}$
$2Pb0 \cdot Si0_2$	6.03	14.68	40
	4.29	20.68	$\boldsymbol{6}$
	3.71	23.96	25
	3.56	25.00	18
	3.22	27.68	100
	3.13	28.50	85
	3.00	29.76	60
	2.95	30.27	20
	2.89	30.92	20
	2,80	31.94	35
	2.58	34.74	20
	2.55	35.16	25
	2.43	36.96	14
	2.41	37.28	10
	2.37	37.93	18
	2, 23	40.41	14
$\alpha$ -4Pb0·Si0 <sub>2</sub>	3.64	24,40	40
	3.36	26.50	40
	3.10	28.78	100
	3.03	29.46	80
	2.91	30.70	40
	2.83	31.58	60
	2.70	33.16	60
	2.49	36.04	40
	2.31	38.96	40
	2.25	40.04	40

**Appendix V, Cont'd.**

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 $\mathcal{A}^{\mathcal{A}}$ 

Element or Compound	$a_{hkl}$ $A^{\mathbf{O}}$	$2\theta$ $\circ$	Relative Intensity
$\gamma$ -4Pb0.Si0 <sub>2</sub>	3.22	27.68	" WITH THE TANK IT IS TO THE THE TABLE TO THE HOLD TO A RECOVER AND THE REAL 6
	3.12	28.58	100
	3.02	29.55	35
	2.95	30.27	18
	2.92	30.59	16
	2.72	32,90	20
	2.66	33.66	6
	2.54	35,30	4
	2.49	36.04	6
	1.961	46.26	4

**Appendix V. Cont1d.**

		؞	
Compound	$d_{hk1}$ $\overline{O}$ A	$2\theta$ , $\circ$	Relative Intensity
$Pb0 \cdot Sb_20_3$	3.601	24.70	W
	3.361	26.50	W
	3.246	27.45	<b>VS</b>
	3.025	29.50	$\mathbf m$
	2.673	33.50	W
	2.635	34.00	W
$Pb0 \cdot Si0_2$	3.527	25,23	${\bf m}$
	3.500	25.43	${\bf m}$
	3.304	26.96	${\mathfrak m}$
	3.193	27.92	m
	3.062	29.14	VvI
	3.012	29.63	W
	2.953	30.24	W
	2,885	30.97	W
	2.558	31.30	VW
	2,779	32.18	W
	2.699	33.16	W
	2.650	33,80	<b>VV</b>
	2.329	38.62	s
	2.281	39.48	VS
	2.189	41.20	VW
	2.046	44.22	W
	2.018	44.88	W

**Appendix VI, Reference X-ray Powder Diffraction Data for** Pb0 $\cdot$ Sb<sub>2</sub>0<sub>3</sub> and Pb0 $\cdot$ Si0<sub>2</sub>

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Appendix VII. Calculation of  $\Delta G^O$  for the Reaction  $Pb0$  (s) =  $Pb0$  (1) below the Melting Point of Pb0.

The melting point of Pb0 =  $1170^{\circ}$ K and  $\Delta H_f^{\circ}$  = 6,110 cal/mole (Rodigina, Gomel'skii, and Luginina, 1961, p. 1801).

$$
\Delta G_{f}^{O} = \Delta H_{f}^{O} - T \Delta S_{f}^{O}
$$

$$
\Delta S_{f}^{O} = \frac{\Delta H_{f}^{O}}{T_{f}}
$$

Assuming  $\Delta C_p = 0$ , then  $\Delta G_f^O = \Delta H_f^O - T$   $(\frac{\Delta H_f^O}{T_f}) = 6110 - T$   $(\frac{6110}{1170})$ Therefore,  $\Delta G_f^O = 6110 - 5.23$  T At  $973^{\circ}$ K,  $\Delta G_{f_{973}}^{\circ}$ 

$$
1730y \quad \text{AC}
$$

$$
= 6110 - 5.23 (973) = 6110 - 5080 = 1030 cal
$$

**Appendix VIII. Calculation of AG° for the Reaction**  $Sb(1) = Sb1$  wt % in Pb

**Since Sb in Pb obeys Henry's law up to about 3.9 wt % at 700°C, the following equation applies for a change in standard state from pure liquid Sb to Sb dissolved in Pb at 1 wt % :**

$$
\Delta G_T^{\circ} = RT \ln a_{Sb_1 \le t \le \epsilon} = RT \ln \gamma^{\circ} X_{Sb_1 \le t \le \epsilon}
$$

At 973<sup>O</sup>K,  $\gamma_{\text{Sb}}^{\text{o}} = 0.798$ . This value was obtained by extrapolating the data of Hultgren, Orr, Anderson, and Kelley **(1960, p. 896) and Seitz and DeWitt (19 39, p. 2595).**

$$
X_{\text{Sb}} \text{ at 1 wt } \$ \text{ Sb in Pb} = \frac{\frac{1}{121.76}}{\frac{1}{121.76} + \frac{99}{207.21}} = 0.0136
$$

At  $973^{\circ}$ K,  $\Delta G_{973}^{\circ}$  = (4.58) (973) log (0.798) (0.0136)

 $= 4456(-1.867)$  $\Delta G_{973}^{\circ}$  = -8320 cal

Appendix IX. Determination of  $\Delta H_{\text{R}}^{\text{O}}$  for the Reaction  $Pb0$  (s) =  $Pb0$  (1)

**The literature contains two entirely distinct values** for the heat of fusion of Pb0. Wicks and Block (1963, p. **6 3) report a value of 2,800 cal/mole whereas Rodigina, Gomel\*skii, and Luginina (19 61, p. 1801) report a value of 6,110 cal/mole. The lower value of 2,800 cal/mole represents an average of values obtained from freezing-point depression calculations made on a number of Pb0~Mex0y systems without any direct component activity data.**

By use of the data of Sridhar and Jeffes (1967, p. 50), **a** value for  $\Delta H_{\text{m}}^{\text{O}}$  can be calculated which is the same as **that reported by Rodigina, Gomel\*skii, and Luginina.**

The activity of Pb0 in the Pb0-Si0<sub>2</sub> system has been **determined by Sridhar and Jeffes and has been shown to be temperature-independent above approximately 80 mole** *%* **PbO in the temperature range from 850° to 1050°C. Therefore, the activity of PbO measured at 1000°C should be equal to the activity of PbO calculated from the depression of the freezing point using the phase diagram shown in Figure 29.**

The activity of Pb0 in the Pb0-Si0<sub>2</sub> system, using the **data of Sridhar and Jeffes and Figure 29, is shown in Figure 39 as a function of reciprocal temperature. A cal**culation for  $\Delta H_{\rm m}^{\rm O}$  from the slope of the log  $a_{\rm Pb0}$  versus  $\frac{1}{\rm m}$ curve has been made with the result that  $\Delta H_{\text{R}}^{\text{O}} = 6$ , 110 cal/mole



Figure 39. Log  $a_{Pb0}$  and log  $x_{Pb0}$  Versus Reciprocal Temperature for the Pb0-SiO<sub>2</sub> System

**Appendix IX. Cont'd.**

**of PbO. This value is the sarae as that reported by Rodigina, Gomel1skii, and Luginina, The freezing-point depression as a function of mole fraction of PbO is seen to be nearly tangent to this curve at mole fractions approaching unity.**

**A third curve shown in Figure 39 was plotted from the freezing-point depression of PbO by GiO^ using a value of 2,800 cal/mole of PbO for**  $\Delta H_{m}^{O}$ **.** The discrepancy in the **slope of this curve at mole fractions of PbO approaching unity indicates that the value of 2,800 cal/mole of PbO** for  $\Delta H_m^O$  is much too low.

**The results of this investigation can be compared with those of Sridhar and Jeffes by use of the data presented in Table 14. The activity of PbO, relative to pure,** solid Pb0, in a liquid containing  $14.4$  mole  $8$  Sb<sub>2</sub>0<sub>3</sub> in **equilibrium with a solid solution at 700°C was calculated** to be  $0.964$ . By use of  $T^{}_{\text{b}} = 1789^{\text{O}}K$  and  $\Delta H^{\text{O}}_{\text{Vap}} = 49,350$ **cal/mole of PbO from Rodigina, Gomel1skii, and Luginina, the vapor pressure above pure, liquid PbO can be calculated with the result that,**

**10.790**  $\log p_{\text{ph0}}$  (mm Hg) = 8.909 -  $\frac{m}{p}$ 

Also, **using their values for**  $T_m = 1170^{\circ}K$  **and**  $\Delta H_m^{\circ} = 6$ **, 110 cal/mole of PbO, the vapor pressure above pure, solid PbO** **Appendix IX, Cont1d,**

**can be calculated with the result that,**

 $log p_{pb0}$  (mm Hg) = 10.050 -  $\frac{12.120}{T}$ 

**The calculated activity of PbO given above can now be referred to the pure, supercooled, liquid standard state kby multiplying it by the ratio of the vapor pressure above pure, solid PbO at 700°C to the vapor pressure above pure, supercooled, liquid PbO at 700°C obtained from the above equationss**

$$
a_{\text{Pb0}}_{(1)} = 0.964 \left( \frac{0.00392}{0.00668} \right) = 0.566
$$

**This value is included in Figure 39 and is found to agree with the value of 6,110 cal/mole of PbO reported by Rodigina, Gomel1skii, and Luginina for the heat of fusion of PbO \***

**T 1171**

## **VITA**

**The author was born on February 14, 19 43, in Niagara Falls, New York. He received his primary and secondary education in Ashtabula, Ohio, and Lewiston, New York.**

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